PHYSICAL REVIEW A 95, 053867 (2017)



Absorption and photoluminescence in organic cavity QED

Felipe Herrera^{1,*} and Frank C. Spano^{2,†}

¹Department of Physics, Universidad de Santiago de Chile, Avenida Ecuador 3943, Santiago, Chile ²Department of Chemistry, Temple University, Philadelphia, Pennsylvania 19122, USA (Received 7 December 2016; published 30 May 2017)

Organic microcavities can be engineered to reach exotic quantum regimes of strong and ultrastrong light-matter coupling. However, the microscopic interpretation of their spectroscopic signals can be challenging due to the competition between coherent and dissipative processes involving electrons, vibrations, and cavity photons. We develop here a theoretical framework based on the Holstein-Tavis-Cummings model and a Markovian treatment of dissipation to account for previously unexplained spectroscopic features of organic microcavities consistently. We identify conditions for the formation of dark vibronic polaritons, a class of light-matter excitations that are not visible in absorption but lead to strong photoluminescence lines. We show that photon leakage from dark vibronic polaritons can be responsible for enhancing photoluminescence at the lower polariton frequency, and also can explain the apparent breakdown of reciprocity between absorption and emission in the vicinity of the bare molecular transition frequency. Successful comparison with experimental data demonstrates the applicability of our theory.

DOI: 10.1103/PhysRevA.95.053867

I. INTRODUCTION

The experimental realization of the strong and ultrastrong coupling regimes of cavity quantum electrodynamics with organic matter [1-21] has stimulated interest in the development of cavity-enhanced optoelectronics [9,22-26], quantum nonlinear optical devices [27-30], and chemical reactors [31–33]. In organic microcavities, strong light-matter coupling is possible at room temperature for cavity quality factors as low as $Q \sim 10$ using metallic mirrors [4,15]. These accessible conditions can facilitate experiments on the one hand by eliminating the need to nanofabricate dielectric mirrors with high Q factors, as is the case with inorganic microcavities [34]. On the other hand, organic microcavities with lossy mirrors can also obscure the interpretation of spectral measurements, as the time scales associated with coherent light-matter coupling, photon decay, dipole decay, and vibrational motion can all be comparable. It is thus necessary to develop a theoretical framework that can take into account these competing coherent and dissipative dynamical processes consistently and provide a framework that can be used to interpret a wide variety of spectral measurements.

Early experiments on strong coupling with metallic microcavities by Hobson *et al.* [4] showed the emergence of a strong and narrow emission photoluminescence peak in a region with negligible absorption. Such results were unexpected because reciprocity dictates that a strong emitter should also be a good absorber [35]. Since the sharp emission line was not dispersive and was close to the bare electronic transition frequency, it was attributed to incoherent localized molecular states that could not exchange energy with the cavity field. This point of view was developed within a quasiparticle approach by Litinskaya *et al.* [36–38], who introduced the so-called incoherent exciton reservoir to partially account for the observed photoluminescence spectra [39,40], treating the electron-vibration coupling

perturbatively. However, recent experiments have identified further spectral features in the emission and absorption spectra of organic microcavities [15,41] that cannot be consistently explained by quasiparticle theories [36–38,42]. The conflicts between existing theories and experiments become more pronounced as the Rabi frequency exceeds the intramolecular vibration frequency.

Vibrational replicas in the spectra of molecular crystals inside optical cavities were first reported by Holmes and Forrest [43], for Rabi frequencies smaller than the intramolecular vibration frequency. Several observed features in the photoluminescence signals where captured by a quantum model developed by La Rocca et al. [44,45]. Spano [46] developed a numerical approach to show that allowing the admixture of multiple vibronic transitions could lead to an effective decoupling between electron and vibrational degrees of freedom and also reduce the effect of inhomogeneous broadening. This numerical insight was further developed and generalized in Ref. [33], where we introduced conditions under which electronic and vibrational degrees of freedom in the lower and upper polariton states become effectively decoupled for all energy disorder configurations. The main condition for establishing this so-called polaron decoupling regime [33] is that the Rabi coupling $\sqrt{N}\Omega$ must exceed the vibronic coupling strength $\lambda^2 \omega_v$ for molecular ensembles with large N. Signatures of polaron decoupling in the lower polariton state could be resolved for ratios as small as $\sqrt{N}\Omega/\lambda^2\omega_{\rm v}\approx 3$, in systems with small disorder and weak vibronic coupling. One direct consequence of polaron decoupling is the reduction of the reorganization energy of excited electrons, which could be exploited to enhance electron transfer reaction rates [33]. Subsequent variational approaches for the description of the lower polariton state [47,48] have confirmed the emergence of polaron decoupling in molecular ensembles.

The theoretical tool that has improved our understanding of strongly coupled organic microcavities is the so-called Holstein-Tavis-Cummings (HTC) model, first introduced by Ćwik *et al.* [49] to study polariton condensation with molecular ensembles. The model combines concepts from condensed

^{*}felipe.herrera.u@usach.cl

[†]spano@temple.edu

matter physics [50,51] and quantum optics [52], by treating the quantized electronic, nuclear, and photon degrees of freedom on equal footing, under the rotating-wave approximation for the cavity-matter coupling. This fully quantized theory generalizes alternative approaches that treat the nuclear degrees of freedom classically [29,30,53], as well as quasiparticle theories that treat the electron-vibration coupling perturbatively [36–38,54]. The HTC model has a rich vibronic polariton structure in the frequency region between the conventional lower and upper polariton transmission doublet [33,46], but in order to build a complete theoretical framework for the interpretation of organic microcavity spectroscopy, it is also necessary to treat the dissipative dynamics of organic polaritons consistently.

In Ref. [55], we introduce an open quantum systems approach to compute the absorption and photoluminescence spectra of organic microcavities and successfully compare our theory with experiments. In this work, we further elaborate on the technical aspects the theory, providing additional insights into the formal structure of the HTC model, the associated vibronic polariton eigenstates, and the modeling of spectroscopic observables. We finally discuss possible improvements of the developed theory and propose experiments to test our predictions.

II. HOLSTEIN-TAVIS-CUMMINGS MODEL

We consider an ensemble of *N* organic emitters inside an optical cavity, which can be either individual molecules or molecular aggregates. The system can be described by the Holstein-Tavis-Cummings (HTC) Hamiltonian [33,46–49], which reads

$$\begin{split} \hat{\mathcal{H}} &= \omega_c \, \hat{a}^\dagger \hat{a} \\ &+ \omega_{\rm v} \sum_{n=1}^N \hat{b}_n^\dagger \hat{b}_n + \sum_{n=1}^N [\omega_e + \omega_{\rm v} \lambda (\hat{b}_n + \hat{b}_n^\dagger)] |e_n\rangle \langle e_n| \\ &+ (\Omega/2) \sum_{n=1}^N (|g_n\rangle \langle e_n| \hat{a}^\dagger + |e_n\rangle \langle g_n| \hat{a}), \end{split} \tag{1}$$

where $\omega_e = \omega_{00} + \omega_{\rm V} \lambda^2$ is the vertical Frank-Condon transition frequency, with ω_{00} being the frequency of the zero-phonon (0-0) vibronic transition, $\omega_{\rm V}$ is the intramolecular vibrational frequency, and λ^2 is the Huang-Rhys factor [51], which quantifies the strength of vibronic coupling. The operator \hat{b}_n annihilates one quantum of vibration on the *n*th chomophore. The operator \hat{a} annihilates a cavity photon at frequency ω_c , and Ω is the single-particle vacuum Rabi frequency, which can be on the order of 100 meV in plasmonic nanocavities [56]. In microcavities, collective couplings $\sqrt{N}\Omega \sim 0.7 - 1.0$ eV have been reported [11,12].

In microcavities, the photon frequency ω_c depends on the in-plane wave vector k_{\parallel} of the cavity mode. The HTC model in Eq. (1) implicitly assumes that all molecular transitions couple equally strong to photons having a specific value of k_{\parallel} . This can only be justified for lossy microcavities near $k_{\parallel}=0$ (normal incidence), where the photon dispersion cannot be resolved within the cavity linewidth. Despite this simplification, we will consider the polariton structure of the HTC model for

higher in-plane momenta $k_{\parallel} > 0$ in later sections. Throughout this work, we assume that the cavity detuning, defined as $\Delta \equiv \omega_{00} - \omega_c$, vanishes exactly at normal incidence.

We ignore energetic disorder in Eq. (1), since for parameters consistent with experimental data [4,39–41], we find that the inhomogeneous broadening associated with energy disorder does not contribute significantly to the overall absorption and emission lineshapes [55]. Within the HTC model, all molecules in the ensemble couple equally strong to the electric field of the near-resonant cavity mode \mathbf{E}_c , which ignores the possibility of molecules being oriented in the sample such that the product $\boldsymbol{\mu} \cdot \mathbf{E}_c$ is negligibly small. We expect such uncoupled molecules to behave as free-space emitters, possibly exhibiting a cavity-enhanced emission rate typical of the weak cavity-matter coupling regime [57]. The theory we develop in the following sections applies only to those emitters in the sample for which the HTC model provides an accurate description of their photophysics.

A. Symmetry of the resonant HTC model

Before proceeding with the detailed analysis of the eigenstates of the HTC model, we introduce a unique symmetry transformation \hat{S} that is shown to commute with the HTC Hamiltonian $\hat{\mathcal{H}}$ in Eq. (1). In this section we define the transformation \hat{S} and prove some of its basic properties for the single-particle and many-particle cases.

For a single emitter (N=1), we can rewrite the light-matter coupling term of the HTC Hamiltonian $\hat{\mathcal{H}}$ by expanding the dipole transition and cavity field operators in the basis spanned by the states $|g|_{\mathcal{V},1_c}\rangle$ and $|e|_{\mathcal{V},0_c}\rangle$, which represent, respectively, a molecule in its ground electronic state $|g\rangle$ with vibrational eigenstate $|v\rangle$ ($v=0,1,2,\ldots$) and one cavity photon, and a molecule in the excited electronic state $|e\rangle$, with vibrational eigenstate $|\tilde{v}\rangle$ in the cavity vacuum. The tilde overstrike indicates that the vibrational eigenstate has \tilde{v} vibrational quanta in the excited-state harmonic nuclear potential, whose minimum is shifted relative to the ground-state potential minimum by a quantity λ along a dimensionless vibrational coordinate [35,51]. The resulting light-matter interaction Hamiltonian reads

$$\hat{H}_{LM} = \frac{1}{2} \sum_{\nu\nu'} \Omega_{\tilde{\nu}'\nu} |e\tilde{\nu}'0_c\rangle \langle g\nu 1_c| + \Omega_{\nu\tilde{\nu}'} |g\nu 1_c\rangle \langle e\tilde{\nu}'0_c|, \quad (2)$$

where $\Omega_{\tilde{\nu}'\nu} = \langle \tilde{\nu}' | \nu \rangle \Omega$ is a vibronic Rabi frequency, weighted by the vibrational overlap factor $\langle \tilde{\nu}' | \nu \rangle$. We introduce the composite symmetry transformation \hat{S} , defined as

$$\hat{S} = \hat{\sigma}_x \hat{Q}_a \hat{D}_g^{\dagger}(\lambda) \hat{D}_e^{\dagger}(-\lambda) \hat{\Pi}_g \hat{\Pi}_e, \tag{3}$$

where $\hat{\Pi}_g$ and $\hat{\Pi}_e$ are the usual parity and displaced parity operators

$$\hat{\Pi}_g = e^{i\pi b^{\dagger}b} \ , \ \hat{\Pi}_e = e^{i\pi \tilde{b}^{\dagger}\tilde{b}}, \tag{4}$$

acting on vibrational eigenstates of the ground- and excited-state potentials as $\hat{\Pi}_g | \nu \rangle = (-1)^{\nu} | \nu \rangle$ and $\hat{\Pi}_e | \tilde{\nu}' \rangle = (-1)^{\nu'} | \tilde{\nu}' \rangle$. The displacement operators have the usual

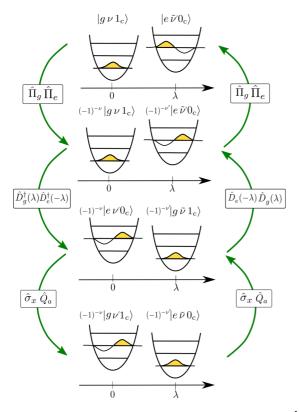


FIG. 1. Stepwise illustration of the symmetry transformation \hat{S} on an arbitrary vibronic configuration involving the ground and excited electronic potentials. The cavity is assumed to be resonant with the electronic transition frequency. The downward arrows represent the action of \hat{S} and the upward arrows its inverse. The horizontal axis represent the dimensionless vibrational coordinate.

definition ($Im[\lambda] = 0$)

$$\hat{D}(\lambda) = e^{\lambda(b^{\dagger} - b)},\tag{5}$$

such that displaced harmonic oscillator eigenstates are defined as $|\tilde{v}\rangle = \hat{D}^{\dagger}(\lambda)|v\rangle$ [35]. The definition of \hat{S} also includes the Pauli matrix σ_x in the $\{|e\rangle,|g\rangle\}$ basis, i.e., $\hat{\sigma}_x = |g\rangle\langle e| + |e\rangle\langle g|$ as well as the one-photon cavity quadrature operator $\hat{Q}_a = |1_c\rangle\langle 0_c| + |0_c\rangle\langle 1_c|$, in the truncated Fock space. By construction, the symmetry transformation \hat{S} is unitary, i.e., $\hat{S}^{\dagger}\hat{S} = 1$, as illustrated in Fig. 1.

We prove in Appendix A that the transformation \hat{S} commutes with the light-matter term \hat{H}_{LM} . Therefore, an eigenstate $|\epsilon_j\rangle$ of the light-matter term \hat{H}_{LM} is a simultaneous eigenstate of \hat{S} , satisfying the eigenvalue equation $\hat{S}|\epsilon_j\rangle = s_j|\epsilon_j\rangle$, with $s_j^2 = 1$. We can thus classify the eigenstates of \hat{H}_{LM} according to the symmetry eigenvalue s_j . However, the total system Hamiltonian $\hat{\mathcal{H}}$ also includes diagonal terms that describe the bare cavity photon and molecular degrees of freedom, and their commutation properties with the symmetry transformation \hat{S} also need to be established. These diagonal terms can be written in the basis described above as

$$\hat{\mathcal{H}} - \hat{H}_{LM} = \sum_{\nu=0,1,\dots} (\omega_c + \nu \omega_{\nu}) |g \nu 1_c\rangle \langle g \nu 1_c|$$

$$+ \sum_{\tilde{\nu} = 0,1} (\omega_{00} + \tilde{\nu} \omega_{\nu}) |e \tilde{\nu} 0_c\rangle \langle e \tilde{\nu} 0_c|. \quad (6)$$

Equation (6) shows that under conditions of exact cavitymatter resonance, i.e., $\omega_{00} = \omega_c$, we also have

$$[(\hat{\mathcal{H}} - \hat{H}_{\text{LM}}), \hat{S}] = 0 = [\hat{\mathcal{H}}, \hat{S}].$$

In other words, under exact resonance the eigenstates of the HTC model for N=1 are also eigenstates of the symmetry transformation \hat{S} , and the HTC Hamiltonian matrix can be factorized into block-diagonal submatrices that conserve the symmetry eigenvalue s.

For many-particle systems ($N \ge 2$), the internal degrees of freedom of the nth particle in the ensemble can be still be associated with a symmetry transformation \hat{S}_n of the form in Eq. (3). Many-particle eigenstates of the HTC model $|\epsilon_j\rangle$ can thus be classified according to the composite transformation \hat{S}_{α} that takes into account the symmetry of the many-body electronic state under permutations of the molecules in the ensemble. One possible choice relevant for the one-excitation manifold is

$$\hat{S}_{\alpha} = \sum_{n=1}^{N} c_{\alpha n} \hat{S}_{n},\tag{7}$$

where the set of orthonormal coefficients $c_{\alpha n}$ encode the symmetry under particle permutations, characterized the quantum number α .

B. Symmetry classification of diabatic vibronic polaritons

For individual particles (N = 1), it proves convenient to introduce diabatic vibronic polaritons of the form

$$|\nu_{\pm}\rangle = \frac{1}{\sqrt{2}}(|e\,\tilde{\nu}\,0_c\rangle \pm |g\,\nu\,1_c\rangle),\tag{8}$$

with $\tilde{v} = v$, which become accurate polariton eigenstates of the system Hamiltonian $\hat{\mathcal{H}}$ for $\sqrt{N}\Omega/\omega_v \ll 1$ [44,58]. From the definition of \hat{S} in Eq. (3), the following relations hold:

$$\hat{S}|\nu_{+}\rangle = (-1)^{\nu}|\nu_{+}\rangle,\tag{9}$$

$$\hat{S}|\nu_{-}\rangle = (-1)^{\nu+1}|\nu_{-}\rangle,$$
 (10)

which are eigenvalue relations with eigenvalues $s_j = \pm 1$, depending on the vibrational configuration. We refer to those diabatic states with eigenvalue s = 1 as even vibronic polaritons and those with s = -1 as odd vibronic polaritons.

As an example, let us consider the system Hamiltonian $\hat{\mathcal{H}}$ for N=1, in a truncated subspace spanned by the diabatic polariton states $\{|0_{\pm}\rangle, |1_{\pm}\rangle, |2_{\pm}\rangle\}$. This basis set splits according to the symmetry eigenvalue s into an even subspace $\mathcal{S}_{+} = \{|0_{+}\rangle, |1_{-}\rangle, |2_{+}\rangle\}$ and an odd subspace $\mathcal{S}_{-} = \{|0_{-}\rangle, |1_{+}\rangle, |2_{-}\rangle\}$. The single-molecule Hamiltonian matrix under exact resonance $(\omega_{c} = \omega_{00})$ can thus be written in the

block-diagonal form

$$\hat{\mathcal{H}}/\omega_{v} = \begin{pmatrix} \bar{\Omega}_{0\bar{0}} & \bar{\Omega}_{0\bar{1}} & \bar{\Omega}_{0\bar{2}} & 0 & 0 & 0\\ \bar{\Omega}_{0\bar{1}} & 1 - \bar{\Omega}_{1\bar{1}} & \bar{\Omega}_{1\bar{2}} & 0 & 0 & 0\\ \bar{\Omega}_{0\bar{2}} & \bar{\Omega}_{1\bar{2}} & 2 + \bar{\Omega}_{2\bar{2}} & 0 & 0 & 0\\ 0 & 0 & 0 & -\bar{\Omega}_{0\bar{0}} & \bar{\Omega}_{0\bar{1}} & \bar{\Omega}_{0\bar{2}}\\ 0 & 0 & 0 & \bar{\Omega}_{0\bar{1}} & 1 + \bar{\Omega}_{1\bar{1}} & \bar{\Omega}_{1\bar{2}}\\ 0 & 0 & 0 & \bar{\Omega}_{0\bar{2}} & \bar{\Omega}_{1\bar{2}} & 2 - \bar{\Omega}_{2\bar{2}} \end{pmatrix}, \tag{11}$$

where $\bar{\Omega}_{\nu\bar{\nu}} = (\Omega/2\omega_{\nu}) \langle \nu | \bar{\nu} \rangle$ are vibronic Rabi frequencies in units of the vibrational frequency ω_{ν} . We have set the zero of energy to be at the cavity frequency ω_c , which corresponds to a rotating frame transformation [59].

The even parity sub-block in Eq. (11) (on the upper left) includes the conventional diabatic upper polariton. As we discuss below, this sub-block supports a zero-energy eigenvalue. The odd parity sub-block (lower right) involves the conventional lower polariton. The off-diagonal couplings within a given sub-block admix diabatic polaritons associated with different molecular vibronic transitions, such that the number of vibrational quanta in the grounds and excited-state harmonic nuclear potentials is not conserved. This admixture becomes significant for Rabi couplings $\Omega/\omega_v \approx 2$.

III. DARK VIBRONIC POLARITONS

We introduce the concept of a dark vibronic polariton [55] to describe eigenstates of the Holstein-Tavis-Cummings model $|\epsilon_i\rangle$ for which we have

$$\mu_{Gi} = \langle G | \hat{\mu} | \epsilon_i \rangle = 0, \tag{12}$$

with $|G\rangle \equiv |g_1 \, 0_1, g_2 \, 0_2, \dots, g_N \, 0_N\rangle |0_c\rangle$ being the absolute ground state of the organic cavity, having no electronic, vibrational, or cavity excitations, for a dipole operator written as $\hat{\mu} = \mu(\hat{\mu}^{(+)} + \hat{\mu}^{(-)})$, where

$$\hat{\mu}^{(+)} = \sum_{n=1}^{N} |g_n\rangle\langle e_n|, \tag{13}$$

with $\hat{\mu}^{(-)} = [\hat{\mu}^{(+)}]^{\dagger}$. The molecular transition dipole moment μ is assumed identical for each emitter. Absorption of light from bound dielectric or surface modes of the microcavity [57,60] by the jth polariton eigenstate is proportional to $|\mu_{Gj}|^2$, just as in free space spectroscopy [51]. Dark vibronic polaritons are therefore invisible in bound-mode absorption at their eigenfrequencies ω_j , which does not prevent them from emitting light in photoluminescence, as we discuss in detail below.

We identify two types of dark vibronic polaritons: X and Y types [55]. The main distinguishing feature between these two types of polariton eigenstates is the degeneracy of their eigenfrequencies: while X-type vibronic polaritons are nondegenerate, Y-type states are (N-1)-fold degenerate. We show below that although X-type dark vibronic polaritons can be partially visible in conventional microcavity absorption measurements, dark vibronic polaritons of the Y type remain invisible for any type of absorption measurement, as long as $k_{\rm b}T/\omega_{\rm v}\ll 1$, which is typical at room temperature.

A. Single-particle states

Before discussing the structure of dark vibronic polaritons of the *X* and *Y* type in more detail, we need to define diabatic single-particle and two-particle material and polariton states. These are illustrated in Fig. 2. Single-particle *material* states represent a molecular ensemble hosting a single vibronic *or* vibrational excitation, or in the language of ordered molecular aggregates, a single exciton or phonon. We represent single-particle vibronic material states as

$$|\alpha, \tilde{\nu}, 0_c\rangle = \sum_{n=1}^{N} c_{\alpha n} |g_1 0_1, \dots, e_n \tilde{\nu}_n \dots g_N 0_N, 0_c\rangle, \qquad (14)$$

where α is a quantum number associated with permutation symmetry of the electronic degrees of freedom, such that the expansion coefficients satisfy $|c_{\alpha n}|^2 = 1/N$, i.e., all molecules are equally likely to host the vibronic excitation \tilde{v} in state $|e\rangle$. There are thus N possible values of α . In the language of molecular aggregates with translational invariance [51], the quantum number α coincides with the exciton quasimomentum k, which can take N possible values given by multiple integers of $2\pi/Na_L$, where a_L is the lattice constant. For organic cavities, however, there is no such translational symmetry as each emitter is randomly located in the sample. Permutation symmetry thus emerges from the fact that within the Holstein-Tavis-Cummings model, all molecules in the ensemble are equally coupled to the confined electric field of the microcavity. In quantum optics, this permutation symmetry

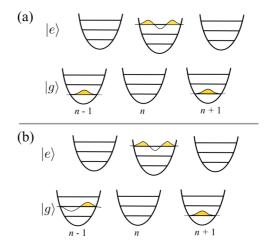


FIG. 2. (a) Displaced-potential representation of a single-particle material state, having a vibronic excitation $|e_n \tilde{v}_n = 2\rangle$ on the *n*th molecule of the ensemble. (b) Two-particle material state with a vibronic excitation ($\tilde{v} = 2$) on molecule *n* and a vibrational excitation (v = 1) on molecule v = 1.

is also known to emerge from the Tavis-Cummings model with homogeneous couplings [52], when represented in the collective spin angular momentum basis [61].

Following Ref. [33], we distinguish states whose electronic degrees of freedom are totally symmetric with respect to particle permutation by the quantum number $\alpha = \alpha_0$, such that $c_{\alpha_0n} = 1/\sqrt{N}$ for all n. For molecular aggregates, this would correspond to a k=0 exciton, which is super-radiant for J aggregates [62]. In the HTC model, only single-particle states with quantum number α_0 can directly exchange energy with the cavity field, under the assumption of homogeneous Rabi coupling. There are thus N-1 single-particle states with $\alpha \neq \alpha_0$ that are not totally symmetric with respect to permutations and thus do not couple directly to the cavity field. These states are the cavity analogs of the $k \neq 0$ excitons in molecular aggregates, which do not couple to light directly, but can be involved in nonradiative processes [51].

The Holstein-Tavis-Cummings model in Eq. (1) can resonantly couple the totally symmetric single-particle material states $|\alpha_0, \tilde{\nu}, 0_c\rangle$ with a vibrationless single-photon state to give a diabatic vibronic *polariton* state of the form

$$|P_{\tilde{v}}^{\pm}\rangle = \frac{1}{\sqrt{2}}(|\alpha_0, \tilde{v}, 0_c\rangle \pm |g_1 0_1, g_2 0_2, \dots, g_N 0_N, 1_c\rangle), \quad (15)$$

with diabatic energies

$$E_{\tilde{v}}^{\pm} = \tilde{v}\omega_{v} \pm \sqrt{N}\Omega|\langle 0|\tilde{v}\rangle|/2. \tag{16}$$

We recover the conventional lower- and upper-polariton states for $\tilde{v} = 0$ [33,46], associated with the polariton splitting $(E_{\tilde{0}}^+ - E_{\tilde{0}}^-) = \sqrt{N}\Omega|\langle 0|\tilde{0}\rangle|$.

B. Two-particle states

Two-particle states represent a configuration where one molecule in the ensemble hosts a vibronic excitation in state $|e\rangle$, while a different molecule hosts a vibrational excitation in state $|g\rangle$. Two-particle states are important to describe the optical spectra of molecular aggregates in free space [51] and in microcavities [46]. Three-particle and multiparticle states can be defined in a similar way, but for the Rabi coupling strengths of interest in this work $\sqrt{N}\Omega/\omega_{\rm v} \leqslant 3$, their contribution to the absorption and emission spectra in the frequency region within the conventional lower and upper polariton doublet is negligible. For larger Rabi couplings, possibly in the ultrastrong coupling regime [11–14,16], such multiparticle excitations should not be ignored [33].

In general, we can represent two-particle vibronic-vibrational material states as

$$|\alpha\beta, \tilde{v}'\nu, 0_c\rangle$$

$$= \sum_{n \neq m} \sum_{m} A_{\alpha n}^{\beta m} |g_1 0_1, \dots, e_n \tilde{v}'_n, \dots, g_m \nu_m, \dots, g_N 0_N, 0_c\rangle,$$
(17)

where the amplitude $A_{\alpha n}^{\beta m}$ is defined by the permutation symmetry quantum number of the electronic degrees of freedom α , and also the permutation quantum number of the vibrational configuration β , for $\nu > 0$. The definition in Eq. (17) involves N(N-1) possible vibronic-vibrational configurations.

Let us write the light-matter term of the HTC model \hat{H}_{LM} in terms of the totally symmetric electronic state $|\alpha_0\rangle = \sum_{l=1}^{N} |e_l\rangle/\sqrt{N}$ as [33]

$$\hat{H}_{LM} = \frac{\sqrt{N}\Omega}{2} (|\alpha_0\rangle\langle g_1, g_2, \dots, g_N|\hat{a} + \text{H.c.}), \qquad (18)$$

where we have simply changed to a collective electronic basis in Eq. (1). We can use this form of \hat{H}_{LM} to understand what photonic states couple to the two-particle material states defined in Eq. (17). For example, we have

$$\langle g_1 0_1, \dots, g_N 0_N, 1_c | \hat{H}_{LM} | \alpha \beta, \tilde{\nu}' \nu, 0_c \rangle = 0, \tag{19}$$

which by the arguments in Appendix B implies that the state $|\alpha\beta, \tilde{\nu}'\nu, 0_c\rangle$ has no transition dipole moment to the absolute ground state of the cavity. In general, two-particle material states can couple to single-photon states having $\nu \geqslant 1$ vibrational excitations, given by

$$|\beta, \nu, 1_c\rangle = \sum_{n=1}^{N} c_{\beta n} |g_1 0_1, \dots, g_n \nu_n, \dots, g_N 0_N, 1_c\rangle,$$
 (20)

representing a single-cavity photon state dressed by a collective vibrational excitation with permutation quantum number β . The associated light-matter coupling element is given by

$$\langle \beta', \nu, 1_c | \hat{H}_{LM} | \alpha \beta, \tilde{\nu}' \nu, 0_c \rangle = \frac{\Omega}{2} \langle 0 | \tilde{\nu}' \rangle \sum_{m} \sum_{l \neq m} c_{\beta' m}^* A_{\alpha l}^{\beta m},$$
(21)

where the double summation contains N(N-1) terms. This expression can be considered as a type of selection rule for the light-matter coupling between two-particle material states and vibrationally dressed photon states. We focus here on those two-particle material states for which the vibronic configuration is totally symmetric under particle permutations; i.e., we set $\alpha = \alpha_0$ in Eq. (17) and

$$A_{\alpha_0 n}^{\beta m} = \frac{c_{\beta m}}{\sqrt{N-1}},\tag{22}$$

for all n. Inserting this expression in Eq. (21) gives

$$\langle \beta', \nu, 1_c | \hat{H}_{LM} | \alpha_0 \beta, \tilde{\nu}' \nu, 0_c \rangle = \sqrt{N - 1} \left(\frac{\Omega}{2} \right) \langle 0 | \tilde{\nu}' \rangle \delta_{\beta \beta'}.$$
(23)

The Kronecker δ factor $\delta_{\beta\beta'}$ is the cavity analog of phonon momentum conservation in systems with translational invariance.

In general, two-particle material states with nonsymmetric vibronic configurations ($\alpha \neq \alpha_0$) can couple with vibration-photon states according to the matrix element in Eq. (21). However, we find that the Rabi splittings associated with nonsymmetric vibronic configurations are much smaller than the Rabi splittings associated with the totally symmetric configuration defined by Eq. (22). We therefore neglect the states in Eq. (17) for which $\alpha \neq \alpha_0$ from our analysis. Numerical tests confirm that such two-particle material states with nonsymmetric vibronic configurations represent a negligible contribution to the polariton eigenstates in the frequency region of the conventional lower and upper single-particle polaritons.

The coupling in Eq. (23) between two-particle *material* states $|\alpha_0\beta, \tilde{v}'v, 0_c\rangle$ and vibrationally excited single-photon

states of the cavity gives rise to diabatic two-particle *polariton* states [46] of the form

$$|P_{\nu\tilde{\nu}'}^{\pm},\beta\rangle = \frac{1}{\sqrt{2}}(|\alpha_0\beta,\tilde{\nu}'\nu,0_c\rangle \pm |\beta,\nu,1_c\rangle),\tag{24}$$

where the first term in the superposition is given by Eqs. (17) and (22). On resonance ($\omega_c = \omega_{00}$), these two-particle polaritons have the diabatic energies

$$E_{\nu\tilde{\nu}'}^{\pm} = (\tilde{\nu}' + \nu)\omega_{\nu} \pm \sqrt{N - 1} \Omega |\langle 0|\tilde{\nu}'\rangle|/2, \qquad (25)$$

which split into a lower (minus sign) and upper (plus sign) diabatic polariton manifold, each being N-fold degenerate according to the N energetically equivalent choices of the permutation quantum number β . The diabatic two-particle polaritons in Eq. (24) can become accurate eigenstates of the HTC Hamiltonian for $\sqrt{N}\Omega/\omega_{\rm v}\ll 1$.

For the symmetric quantum number $\beta=\alpha_0$, the two-particle diabatic vibronic polariton $|P_{\nu\bar{\nu}'}^{\pm},\alpha_0\rangle$ [Eq. (24)] can couple to conventional single-particle polaritons $|P_{\bar{\nu}'}^{\pm}\rangle$ [Eq. (15)] by the light-matter term according to the matrix elements

$$\langle P_{\tilde{\nu}'}^{\pm}|\hat{H}_{LM}|P_{\nu\tilde{\nu}'}^{+},\alpha_{0}\rangle = \frac{\Omega}{4}\langle \tilde{\nu}'|\nu\rangle, \tag{26}$$

$$\langle P_{\tilde{\nu}'}^{\pm}|\hat{H}_{\rm LM}|P_{\nu\tilde{\nu}'}^{-},\alpha_{0}\rangle = -\frac{\Omega}{4}\langle \tilde{\nu}'|\nu\rangle, \tag{27}$$

independent of the number of molecules N.

We conclude this section by noting that the Holstein-Tavis-Cummings model also allows the coupling between single-particle material states $|\alpha \neq \alpha_0, \tilde{\nu}, 0_c\rangle$ [Eq. (14)] that are not totally symmetric with respect to permutation, with vibrationally excited photon states $|\beta, \nu, 1_c\rangle$. Such coupling preserves the permutation symmetry quantum number, i.e.,

$$\alpha = \beta \neq \alpha_0. \tag{28}$$

resulting in the nonzero HTC matrix element

$$\langle \alpha, \tilde{\nu}', 0_c | \hat{H}_{LM} | P_{\nu \tilde{\nu}'}^{\pm}, \beta \rangle = \pm \delta_{\beta \alpha} \frac{\langle \nu | \tilde{\nu}' \rangle}{\sqrt{2}} \left(\frac{\Omega}{2} \right),$$
 (29)

also independent of N. This expression is valid for the (N-1) possible values of $\alpha \neq \alpha_0$ (nonsymmetric superpositions). As a consequence of this coupling, the otherwise dark collective electronic excitations $|\alpha \neq \alpha_0, \tilde{\nu}, 0_c\rangle$ can admix with two-particle polariton states $|P^{\pm}_{\nu\tilde{\nu}'}, \alpha\rangle$ given by Eq. (24), to borrow a photonic component with $\nu \geqslant 1$ vibrational quanta. As we discuss below, such admixture can be significant in the Rabi coupling regime $\sqrt{N}\Omega/\omega_{\nu}\approx 2$, where the states involved in the mixing become quasidegenerate.

C. Dark vibronic polaritons of the X type

We are interested in the eigenstates of the HTC Hamiltonian $\hat{\mathcal{H}}$ [Eq. (1)], which have energies close to the bare molecular transition frequency, given the unexpectedly strong cavity emission and weak absorption observed in this frequency region [4,39–41]. In the rotating frame of the resonant cavity mode, a polariton state at the bare molecular frequency satisfies

$$\hat{\mathcal{H}}|X\rangle = 0. \tag{30}$$

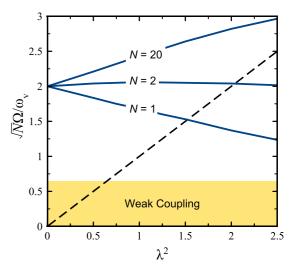


FIG. 3. HTC model parameters. Solid lines are the parameters for which we can define the zero-energy dark vibronic polariton $|X\rangle$, for different molecule numbers N, where N=20 is representative of the thermodynamic limit [47]. The dashed line shows the threshold for polaron decoupling of the lower polariton state, defined as $\sqrt{N}\Omega/\lambda^2\omega_v=1$ for $N\gg1$. λ^2 is the Huang-Rhys factor and ω_v is the intramolecular frequency. The shaded region represents the weak coupling regime $\sqrt{N}\Omega\leqslant\kappa$, where $\kappa\sim0.6\,\omega_v$ is a typical photon decay rate for a microcavity with quality factor $Q\sim10$ [4]. The cavity is assumed resonant with the zero-phonon electronic transition at normal incidence.

In Appendix B we prove that indeed for a polariton eigenstate that satisfies Eq. (30), the transition dipole moment to the absolute ground state $\langle G|\hat{\mu}|\epsilon_j\rangle$ must vanish. According to the definition in Eq. (12), the zero-energy polariton state $|X\rangle$ is therefore a dark vibronic polariton, which we call of the X type. We show in Fig. 3 the numerically estimated values of the HTC Hamiltonian parameters $\sqrt{N}\Omega/\omega_v$ and λ^2 for which one of the eigenstates of $\hat{\mathcal{H}}$ satisfies Eq. (30), without degeneracies. For completeness, we also shown in Fig. 3 what we define as the polaron-decoupling threshold of the lower polariton state in molecular ensembles [33], defined by the equality

$$\sqrt{N}\Omega/\lambda^2\omega_{\rm v}=1.$$

For Rabi couplings a few times higher than this threshold, the electronic and vibrational degrees of freedom of the lower polariton state become separable, with deviations from complete separability that scale as $\lambda^2/4N$ [33].

We can understand the emergence of the zero-energy dark vibronic polariton $|X\rangle$ as a destructive interference effect. For N=1, it is not difficult to show that only the even-symmetry sub-block in Eq. (11) can have a zero-energy eigenvalue. Therefore, we can expand the $|X\rangle$ state in a diabatic polariton basis from Eq. (8) to read

$$|X\rangle \approx c_0|0_+\rangle - c_1|1_-\rangle - c_2|2_+\rangle,\tag{31}$$

where $c_{\nu} > c_{\nu+1} > 0$ and $\lambda > 0$. We have assumed the same even-symmetry truncated basis as in Eq. (11). The transition dipole moment μ_{GX} is thus given by

$$\mu_X \approx \mu(c_0\langle 0|\tilde{0}\rangle - c_1\langle 0|\tilde{1}\rangle - c_2\langle 0|\tilde{2}\rangle); \tag{32}$$

i.e., the destructive interference between the vibrational overlap factors associated with the bare 0-0, 0-1, and 0-2 vibronic transitions leads to the vanishing dipole moment for state $|X\rangle$. The destructive interference is more efficient when higher energy polariton states are considered in the basis set.

Figure 3 shows that for any N it is always possible to find values of the HTC model parameters for which Eq. (30) holds, which generalizes the definition of the $|X\rangle$ state in Eq. (31) to the many-particle case. We note that for $N \ge 2$, the zero-energy $|X\rangle$ state also acquires a two-particle polariton character, due to the coupling between the conventional upper polariton state $|P_{\bar{0}}^+\rangle$ with the symmetric two-particle polariton state $|P_{\bar{0}}^-\rangle$. This type of coupling, in addition to the admixture of single-particle polariton states as in Eq. (31), gives rise to a set of *nondegenerate* dark vibronic polaritons that we call of the X type in the frequency region defined by the conventional lower- and upper-polariton doublet.

D. Dark vibronic polaritons of the Y type

Dark vibronic polaritons of the Y type result from the admixture of diabatic two-particle polariton states $|P_{\nu\bar{\nu}'}^-, \beta\rangle$, [Eq. (24)] with nonsymmetric (or dark) material vibronic excitations $|\beta, \tilde{\nu}', 0_c\rangle$, for $\beta \neq \alpha_0$. This coupling is allowed by the light-matter matrix element in Eq. (29), and gives rise to two Y-type dark vibronic polaritons for each of the N-1 nonsymmetric values of β . For example, when $\sqrt{N}\Omega/\omega_v\approx 2$, there are Y-type polariton eigenstates in the spectral region near the bare electronic frequency $(\omega_j\approx 0)$ that can be approximately given by

$$|Y_a\rangle \approx a_1|\beta,\tilde{0},0_c\rangle + a_2|P_{1\tilde{0}}^-,\beta\rangle,$$
 (33)

$$|Y_b\rangle \approx b_1|\beta,\tilde{0},0_c\rangle - b_2|P_{1\tilde{0}}^-,\beta\rangle,$$
 (34)

where a_1, a_2, b_1 , and b_2 are positive real numbers that do not depend on β , since the coupling in Eq. (29) is independent of the permutation quantum number. The states $|Y_a\rangle$ and $|Y_b\rangle$ are thus each (N-1)-fold degenerate. States of this form become important in the description of the photoluminescence spectra.

In Fig. 4, we show a map that visually summarizes the states and couplings involved in the formation of dark vibronic polaritons of the X and Y types, indicating the different levels of light-matter coupling allowed in the homogeneous HTC model: (i) direct coupling of material and vibration-photon states to form diabatic single- and two-particle polaritons, (ii) the coupling of diabatic single- and two-particle polaritons to form nondegenerate X states that are totally symmetric with respect to permutation of vibronic and vibrational degrees of freedom, and (iii) the coupling of nonsymmetric diabatic two-particle polaritons with nonsymmetric collective vibronic excitations (the so-called dark excitons) to form dark vibronic polaritons of the Y type, which are (N-1)-fold degenerate.

IV. DISSIPATIVE POLARITON DYNAMICS

In order to model the dissipative dynamics of organic polaritons in low-Q microcavities, we ignore nonradiative intramolecular relaxation [35] and assume the dissipative dynamics of the polariton density matrix $\hat{\rho}(t)$, which describes the state of the cavity, to be given by the Lindblad quantum

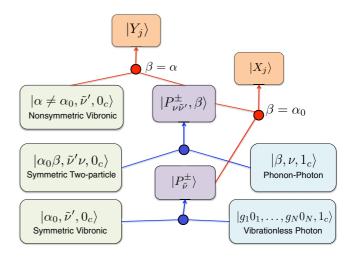


FIG. 4. Illustration of the states (squares) and couplings (circles) involved in the formation of dark vibronic polaritons of the X and Y types. Collective single-particle vibronic excitations and vibrationless photon states couple via the light-matter term in the HTC model to form diabatic single-particle polaritons $|P_{\tilde{v}}^{\pm}\rangle$. Twoparticle diabatic polaritons $|P_{\vec{\nu}'\nu}^{\pm}, \beta\rangle$ arise from the coupling between vibronic-vibrational collective states and a cavity photon dressed by a vibrational collective excitation (phonon). The permutation quantum number of two-particle state is totally symmetric with respect to permutations of the vibronic excitation (quantum number α_0), for any of the N possible quantum numbers β for the vibrational excitation. The states $|P_{\tilde{v}'v}^{\pm}, \beta\rangle$ and $|P_{\tilde{v}}^{\pm}\rangle$ further admix to form nondegenerate *X*-type polaritons when β is totally symmetric ($\beta = \alpha_0$). Each nontotally-symmetric two-particle polariton $|P_{\tilde{\nu}'\nu}^{\pm}, \beta \neq \alpha_0\rangle$ can further couple to the nonsymmetric single-particle vibronic excitations (dark excitons) $|\alpha \neq \alpha_0, \tilde{\nu}', 0_c\rangle$ to form a manifold of N-1 vibronic polaritons of the Y type, preserving the permutation symmetry of vibronic and vibrational excitations ($\alpha = \beta$).

master equation [61,63]

$$\frac{d}{dt}\hat{\rho}(t) = -i[\hat{\mathcal{H}}, \hat{\rho}(t)] + \mathcal{L}_a[\hat{\rho}(t)] + \mathcal{L}_{\mu}[\hat{\rho}(t)]. \tag{35}$$

The first term describes coherent polariton evolution as determined by the Holstein-Tavis-Cummings Hamiltonian \mathcal{H} [Eq. (1)]. The term $\mathcal{L}_a[\hat{\rho}(t)]$ describes the dissipative evolution associated with the loss of cavity photons through the mirrors (cavity leakage), and the term $\mathcal{L}_{\mu}[\hat{\rho}(t)]$ describes the dissipative dynamics associated with radiative dipole decay of the electronic degrees of freedom (fluorescence) into bound modes of the nanostructure. The Lindblad form of the dissipators read [61,63]

$$\mathcal{L}_a[\hat{\rho}(t)] = \frac{\kappa}{2} (2\hat{a}\hat{\rho}\hat{a}^{\dagger} - \{\hat{a}^{\dagger}\hat{a}, \hat{\rho}\}), \tag{36}$$

$$\mathcal{L}_{\mu}[\hat{\rho}(t)] = \sum_{n} \frac{\gamma_{n}}{2} (2\hat{\sigma}_{n}^{-} \hat{\rho}(t)\hat{\sigma}_{n}^{+} - \{\hat{\sigma}_{n}^{+} \hat{\sigma}_{n}^{-}, \hat{\rho}(t)\}), \quad (37)$$

where κ is the empty-cavity decay rate, $\hat{\sigma}_n^- \equiv |g_n\rangle\langle e_n|$ is an electronic transition operator, with $\hat{\sigma}_n^+ = [\hat{\sigma}_n^-]^\dagger$, and $\{\hat{A}, \hat{B}\}$ denotes an anticommutator. The single-emitter decay rate γ_n can be estimated from the classical Green's function of the optical nanostructure [64] and is not necessarily equal to the fluorescence decay rate in free space [65].

We implicitly assume in Eq. (37) that a typical distance between emitters in the ensemble $\langle (\mathbf{x}_n - \mathbf{x}_m) \rangle$ is much larger than the decay length of the equal-time two-point correlation function $\langle \hat{\mathcal{E}}_b^{(-)}(\mathbf{x}_n) \hat{\mathcal{E}}_b^{(+)}(\mathbf{x}_m) \rangle$. If this is not the case, then site nondiagonal terms in the dipole dissipator $\mathcal{L}_{\mu}[\hat{\rho}(t)]$ should be taken into account, as well as coherent long-range interactions between emitters [66]. We made a local-decay assumption here for simplicity.

We can assume that all molecules in the ensemble have identical transition dipole moments, and thus fluorescence rate γ_e , and also that the spectral density of the electromagnetic reservoir does not vary significantly in a frequency range on the order of $\sim \sqrt{N}\Omega$ centered at the cavity frequency ω_c . The latter assumption is not accurate in the ultrastrong coupling regime of cavity-matter coupling [67,68].

By expanding the quantum master equation in Eq. (35) in terms of an eigenbasis of the HTC Hamiltonian $\hat{\mathcal{H}}$, and only including terms that evolve at optical frequencies, we arrive at the polariton master equation

$$\frac{d}{dt}\hat{\rho}(t) = \sum_{ij} \frac{\gamma_{ij}}{2} (2|\epsilon_i\rangle\langle\epsilon_j|\hat{\rho}(t)|\epsilon_j\rangle\langle\epsilon_i| - \{|\epsilon_j\rangle\langle\epsilon_j|, \hat{\rho}(t)\}),$$

where we use a notational convention in which eigenstates $|\epsilon_i\rangle$ belong to the ground electronic state manifold for the ith vibrational configuration of the molecules, and states $|\epsilon_j\rangle$ represent polariton eigenstates (light-matter excitation). The transition frequencies $\omega_{ij} = \epsilon_j - \epsilon_i > 0$ are in the optical regime of interest. The Lindblad (secular) form of the polariton master equation in Eq. (38) describes simple birth-death processes for the populations, as well as decay of polariton coherences $\rho_{ij} \equiv \langle \epsilon_i | \hat{\rho} | \epsilon_i \rangle$ due to radiative relaxation.

From the Lindblad master equation above, we obtain a decay rate for the *j*th polariton eigenstate $\Gamma_j = \sum_i \gamma_{ij}$ (see Appendix D) given by

$$\Gamma_j = \kappa \sum_i |\langle \epsilon_i | \hat{a} | \epsilon_j \rangle|^2 + N \gamma_e \sum_j |\langle \epsilon_i | \hat{J}_- | \epsilon_j \rangle|^2, \quad (39)$$

where we introduced a size-normalized collective transition operator $\hat{J}_{-} = \mu^{(+)}/\sqrt{N}$. This is done for numerical convenience, given the impossibility of simulating microcavities with large $N \gg 10^4$. For a numerically accessible system with finite $N \sim 20$, a normalized dipole decay rate of order unity can be numerically computed and then scaled to realistic values of $N\gamma_e$ in Eq. (39). This is done to get an accurate estimate for the homogeneous spectral linewidth.

V. MODELING ORGANIC CAVITY SPECTROSCOPY

Having described the structure and properties of dark vibronic polaritons of the X and Y types, our goal for the remainder of this article is to understand how dark vibronic polaritons manifest in the absorption and emission spectra of organic microcavities. We focus on the three types of measured signals: absorption through the mirrors $A(\omega)$, bound mode absorption $A_b(\omega)$, and photoluminescence through the mirrors or leakage photoluminescence $S_{LPL}(\omega)$. Bound modes refer to normal modes of the cavity for which the in-plane wave vector exceeds the cutoff for total internal reflection

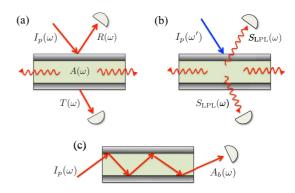


FIG. 5. Spectral signals. (a) Reflection R, transmission T, and absorption A=1-R-T of an external pump $I_p(\omega)$. Absorption is due to spontaneous emission into bound modes of the microcavity. (b) Leakage photoluminescence $S_{\text{LPL}}(\omega)$ following weak laser pumping at frequency $\omega' > \omega$. Bound mode photoluminescence [46] is also shown. (c) Bound mode absorption spectra $A_b(\omega)$, for laser driving beyond cutoff for total internal reflection.

and thus the mode electric field decays exponentially on the outer side of the cavity mirrors. Such bound modes can have plasmonic or purely dielectric character [60,69]. In Fig. 5 we illustrate the spectral measurements described in this work. We do not consider photoluminescence into bound modes of the nanostructure, which was discussed in Ref. [46] for *J* aggregates in microcavities.

Conventional absorption through the mirrors $A(\omega)$ and bound mode absorption $A_b(\omega)$ differ in the way an external pump drives the cavity system. In the former case, a resonant pump laser transfers photons from a free-space electromagnetic mode (monochromatic laser) to the intracavity medium through the partially reflecting mirrors [15]. This photon transfer populates a polariton state $|\epsilon_j\rangle$, which can then decay either by converting an intracavity photon back to an external propagating photon, giving rise to reflection R and transmission T, or by spontaneously emitting a photon into one of the bound modes of the nanostructure [60]. The latter decay channel leads to attenuation of the total reflected plus transmitted field, relative to the input photon flux. Since conservation of photon flux thus requires that R+T+A=1 at all pump frequencies, the conventional absorption spectra is defined as [41]

$$A(\omega_p) = 1 - R(\omega_p) - T(\omega_p), \tag{40}$$

where $R(\omega_p)$ and $T(\omega_p)$ are the reflection and transmission spectra, normalized to the pump intensity at frequency ω_p . In this type of absorption spectra, an external photon must first populate a polariton state, resulting in a dependence of the signal on matrix elements of the operator \hat{a} . Once a polariton is populated, conventional absorption is the result of dipole emission from polaritons into bound modes of the nanostructure, which in turn is determined by matrix elements of the dipole operator $\hat{\mu}$ between polariton states. On the other hand, bound mode absorption $A_b(\omega)$, as well as fluorescence, can directly probe the material polarization $\hat{\mu}$, as the probe field is trapped inside the intracavity medium by total internal reflection [60,69].

In general, nonradiative decay processes involving electronic degrees of freedom also contribute to $A(\omega)$; however,

(38)

the time scales for nonradiative molecular relaxation $\tau_{\rm nr} \sim 1{\text -}10$ ps [35] can be expected to be slower than the radiative time scales $1/\kappa \sim 1/N\gamma_e \sim 10$ fs in low-Q microcavities [4,65].

A. Output spectrum and cavity absorption

The reflection spectra $R(\omega)$ and transmission spectra $T(\omega)$ are given by the spectrum of the electric field operator $\hat{\mathcal{E}}(\mathbf{x},t)$ [$\sqrt{\mathrm{Hz}}$] on either external side of a microcavity driven by a pump photon flux, denoted as $|\langle \hat{F}_1 \rangle|^2$ [Hz], incoming on one side of the cavity. We show in Appendix C, using a Schrödinger picture input-output formalism [61], that if we denote by $\hat{\mathcal{E}}_1$ the field reflected on the same side as the incoming pump field, and by $\hat{\mathcal{E}}_2$ the field transmitted on the other side of the cavity, conservation of photon flux requires that

$$|\langle \hat{\mathcal{E}}_1 \rangle|^2 + |\langle \hat{\mathcal{E}}_2 \rangle|^2 = |\langle \hat{F}_1 \rangle|^2, \tag{41}$$

in steady state. This becomes the usual empty-cavity relation R+T=1 after normalization by the incoming flux. In general, Eq. (41) needs to be integrated over all frequencies to obtain a relation in units of photon number.

For a cavity with an intracavity medium, as discussed above, polariton fluorescence into bound modes leads to attenuation of the reflected and transmitted fields. If we assume that a polariton can emit radiation at a single frequency, photon flux conservation reads

$$|\langle \hat{\mathcal{E}}_b \rangle|^2 + |\langle \hat{\mathcal{E}}_1 \rangle|^2 + |\langle \hat{\mathcal{E}}_2 \rangle|^2 = |\langle \hat{F}_1 \rangle|^2, \tag{42}$$

where $\hat{\mathcal{E}}_b$ is the bound electric field flux operator. Normalizing by the input flux gives Eq. (40). This relation shows that the through-mirror absorption spectra $A(\omega)=1-R(\omega)-T(\omega)$ is determined by the steady-state spectrum of the the bound electric field $S_b(\omega) \propto \int d\tau \langle \hat{\mathcal{E}}_b^{\dagger}(\tau) \hat{\mathcal{E}}_b(0) \rangle e^{i\omega\tau}$, which as shown in Appendix C 2, is proportional to the bound fluorescence spectra

$$S_b(\omega) \propto \int_0^\infty d\tau \langle \hat{\mu}^{(-)}(\tau) \hat{\mu}^{(+)}(0) \rangle e^{i\omega\tau},$$
 (43)

where $\hat{\mu}^{(+)}$ is defined in Eq. (13). Integrating the fluorescence spectra over all emission frequencies gives the total number of photons emitted into the bound modes, after pumping the cavity with a monochromatic field at frequency ω_p . Therefore, the value of the absorption coefficient A at the pump frequency ω_p is given by

$$A(\omega_p) = \int_0^\infty d\omega \int_0^\infty d\tau \, \langle \hat{\mu}^{(-)}(\tau) \hat{\mu}^{(+)}(0) \rangle \, e^{i\omega\tau}, \qquad (44)$$

up to a proportionality factor that depends on the density of states of the electromagnetic field inside the cavity.

In Appendix E, we develop a model to evaluate the spectrum of the dipole fluctuations in Eq. (44), which determine the absorption of a weak pump field at frequency ω_p . The external periodic driving is considered as a perturbation to the Holstein-Tavis-Cummings Hamiltonian $\hat{\mathcal{H}}$, which defines a time-dependent driven HTC model of the form $\hat{H}(t) = \hat{\mathcal{H}} + \hat{V}_p(t)$, where

$$\hat{V}_{p}(t) = \Omega_{p}(\hat{a}^{\dagger} e^{-i\omega_{p}t} + \hat{a} e^{i\omega_{p}t})$$
 (45)

is the periodic driving term with frequency ω_p and amplitude $\Omega_p \ll \sqrt{N}\Omega \ll \omega_c$. We obtain the steady-state polariton population ρ_j of the system in the presence the external driving, to second order in Ω_p . The dipole fluctuations are evaluated within the no-quantum-jump (NQJ) approximation, which we introduce to simplify the quantum regression formula. After performing the time and frequency integrations in Eq. (44), we obtain the expression

$$A(\omega_p) = \pi |\Omega_p|^2 \sum_{i} \frac{|\langle G|\hat{a}|\epsilon_j\rangle|^2 (\kappa_{Gj}/\Gamma_j)}{(\omega_p - \omega_{jG})^2 + \kappa_{Gj}^2} F_j, \qquad (46)$$

where κ_{Gj} is the decay rate for the optical coherence $\rho_{Gj} \equiv \langle G | \hat{\rho} | \epsilon_j \rangle$, which we can allow to account for nonradiative relaxation processes as well (details in Appendix E). We have also defined the total dipole emission strength of the *j*th polariton eigenstate as

$$F_j = \sum_{i} |\langle \epsilon_i | \hat{\mu}^{(+)} | \epsilon_j \rangle|^2. \tag{47}$$

Equation (46) shows that if $F_j=0$ for a given polariton eigenstate $|\epsilon_j\rangle$, there is no resonant absorption at that polariton frequency either. In other words, polaritons that fluorescence poorly into bound modes of the nanostructure cannot attenuate the reflected and transmitted fields efficiently. On the other hand, even when a polariton state $|\epsilon_j\rangle$ can have a strong bound fluorescence, it cannot attenuate the driving field efficiently when its vibrationless photonic component $\langle G|\hat{a}|\epsilon_j\rangle$ is negligible or the pump field is far detuned from ω_{jG} , which suppresses its stationary polariton population ρ_j .

The bound absorption spectrum $A_b(\omega)$ is also given by the Fourier transform of a dipole correlation function as in Eq. (43) for bound fluorescence, thus satisfying the usual reciprocal relation between absorption and emission in free space [35]. The stationary bound absorption spectrum taking the absolute ground state $|G\rangle$ as initial condition is thus given by

$$A_b(\omega) = \sum_j |\langle \epsilon_j | \hat{\mu}^{(-)} | G \rangle|^2 \frac{(\Gamma_j/2)}{(\omega - \omega_{jG})^2 + (\Gamma_j/2)^2}, \quad (48)$$

where *j* labels polariton eigenstates and where Γ_j is given by (39).

B. Cavity photoluminescence

Leakage photoluminescence (LPL) is detected on either side of an organic cavity, as illustrated in Fig. 5. The LPL spectra $S_{\text{LPL}}(\omega)$ is thus directly proportional to the spectrum of the external field operators $\hat{\mathcal{E}}_1(t)$ and $\hat{\mathcal{E}}_2(t)$, at the reflection or the transmission side of the cavity, respectively. As discussed in Appendix C, for a classical (coherent state) input field that is uncorrelated with the intracavity field operator $\hat{a}(t)$, i.e., $\langle \hat{F}_1(t)\hat{a}(t')\rangle \rightarrow 0$, the external field spectrum is directly proportional to the spectrum of the intracavity field fluctuations. Therefore, the stationary leakage PL spectra can be computed as

$$S_{\rm LPL}(\omega) = \int_0^\infty d\tau \, \langle \hat{a}^{\dagger}(\tau) \hat{a}(0) \rangle \, e^{i\omega\tau}, \tag{49}$$

up to a proportionality factor that depends on the density of states of the electromagnetic field. The dependence on the pump frequency enters in the intracavity field autocorrelation dynamics, which we compute from the dissipative dynamics of organic polaritons, together with the quantum regression formula.

We show in Appendix D that the spectrum of the stationary cavity fluctuations in Eq. (49) can be easily evaluated within the NQJ approximation. The resulting expression for the LPL spectra reads

$$S_{LPL}(\omega) = \sum_{ij} \rho_j |\langle \epsilon_i | \hat{a} | \epsilon_j \rangle|^2 \frac{(\Gamma_j/2)}{(\omega - \omega_{ji})^2 + (\Gamma_j/2)^2}, \quad (50)$$

where ρ_j is the steady-state population of the *j*th HTC polariton eigenstate $|\epsilon_j\rangle$, Γ_j is the polariton decay rate from Eq. (39), and $\omega_{ji} = \epsilon_j - \epsilon_i > 0$ is the transition frequency for the optical transition $|\epsilon_i\rangle \rightarrow |\epsilon_i\rangle$.

We compute the LPL emission spectra below by assuming a stationary polariton population of the form $\rho_j = 1/Md_j$, where d_j is the degeneracy of the jth HTC eigenvalue and $M = \sum_j d_j$ is the number of polariton states considered. For a single molecule $d_j = 1$ for all j, but for $N \ge 2$ this is not the case.

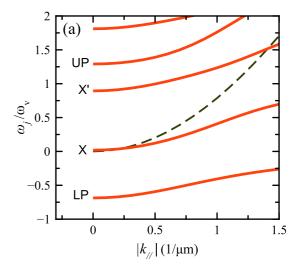
VI. ABSORPTION AND EMISSION OF ORGANIC CAVITIES

We now apply the quantum formalism developed in the previous sections to discuss the absorption and photoluminescence spectroscopy of organic microcavities. Specifically, we will use Eqs. (46), (48) and (50) to respectively evaluate the conventional absorption spectrum, the bound absorption spectrum and the leakage PL spectrum for several cases. We discuss first the case of a single molecule in a cavity (N = 1), then a molecular dimer (N = 2), and finally a molecular ensemble with large N. For the ensemble case, we compare the simulated emission spectra with experimental results from the literature.

A. Single molecule

For a single emitter, the critical Rabi coupling for which the zero-eigenvalue equation (30) can be solved is $\Omega=1.68\,\omega_{\rm v}$ for $\lambda^2=1$, at normal incidence $(k_{\parallel}=0)$. For this choice of Rabi frequency, we show the polariton dispersion in Fig. 6(a). The dispersion of the empty cavity mode $\omega_c(k_{\parallel})$ is shown for comparison (dashed line), where k_{\parallel} is the in-plane wave vector of the cavity mode. For all values of k_{\parallel} shown, the HTC polariton eigenstates have at least 10% photonic character. The zero-energy dark vibronic polariton state $|X\rangle$, which is dispersive in our model, appears in the middle region between the lower (LP) and upper (UP) polariton branches. A second X-type polariton branch, which we denote as $|X'\rangle$, occurs near the upper polariton branch.

Figure 6(b) is a diagram of the allowed transitions from the bottom of each of the polariton branches shown in Fig. 6(a), to the lowest three vibrational states of the ground-state manifold. Arrows indicate allowed transitions between polariton states $|\epsilon_j\rangle$, with frequencies ω_j , and states in the ground manifold $|g,\nu,0_c\rangle$ having $\nu\leqslant 1$ vibrational quanta. Upward arrows are dipole allowed transitions, relevant in bound absorption experiments [57,60]. The energy of the absolute ground state $|g,0,0_c\rangle$ is denoted as ω_g . Emission events are dissipative in



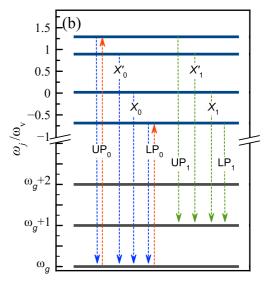


FIG. 6. Single molecule dispersion and allowed transitions. (a) Polariton dispersion for Rabi coupling $\Omega = 1.68 \,\omega_{\rm v}$. For all considered in-plane wave vectors k_{\parallel} , the polariton branches have at least 10% photonic character. (b) Energy level diagram with the arrows indicating allowed transitions from the bottom of the polariton branches in panel (a). Transitions are denoted as P_{ν} , from a polariton state $P = |\epsilon_j\rangle$ at frequency ω_j , into a state of the ground manifold with ν vibrational quanta $|g,\nu,0_c\rangle$. Upward arrows are dipole allowed transitions, relevant in bound absorption experiments, for ω_g being the absolute ground-state energy (vertical axes not on scale). In both panels we set $\lambda^2 = 1$. $\omega_{\rm v}$ is the intramolecular vibration frequency.

the sense that the material is projected into the state $|g, v, 0_c\rangle$ after photon loss through the cavity mirrors (leakage), which can be represented by the mapping

$$\hat{a}|\epsilon_i\rangle \to |g,\nu,0_c\rangle + \hbar\omega.$$
 (51)

The radiated photon is detected at the frequency

$$\omega = \omega_i - \nu \,\omega_{\rm v},\tag{52}$$

so that leakage photoluminescence maps the polariton dispersion $\omega_j(k_{\parallel})$ only for vibrationless transitions ($\nu=0$). For convenience, we denote downward transitions by P_{ν} , where P labels the emitting polariton state $|\epsilon_j\rangle$ and ν is the number

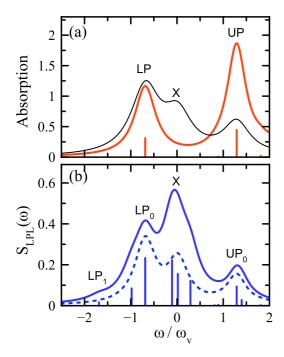


FIG. 7. Cavity absorption and emission for a single molecule (N=1). (a) Conventional absorption A=1-R-T (black line) and bound absorption spectra (red line). The lower polariton (LP) and upper polariton (UP) peaks are present in both types of absorption signals. The zero-energy dark vibronic polariton $|X\rangle$ is not present in bound absorption. (b) Leakage photoluminescence spectra (LPL) for the same parameters as in panel (a). Peak labels have the form P_{ν} , where P refers to the initial polariton state and ν to the vibrational quantum number in the final state of the transition. Dashed and solid lines include transitions with up to $\nu=0$ and $\nu=1$ vibrational quanta, respectively. Vertical bars indicate the position and relative strength of the peak maxima. In both panels we set $\Omega=1.68\,\omega_{\rm v},\ \kappa/\omega_{\rm v}=0.9,\ \gamma_e/\omega_{\rm v}=0.2,\ {\rm and}\ {\rm a}\ {\rm nonradiative}\ {\rm decay}$ rate $\gamma_{\rm nr}/\omega_{\rm v}=0.1$, for $\lambda^2=1$ and $\omega_c=\omega_{00}$ at normal incidence. $\omega_{\rm v}$ is the intramolecular vibration frequency.

of vibrational quanta in the ground manifold after photon leakage. Dissipative transitions of the form $P_{\nu>0}$ are ignored in existing quasiparticle theories of organic microcavities [36–38,42,44,58].

We show in Fig. 7 the simulated absorption and leakage PL emission spectra for a single molecule in a microcavity. Such systems can now be realized experimentally using localized plasmonic fields [56]. The bound absorption spectra is computed from the dipole autocorrelation function as discussed in Appendix D, assuming that only the absolute ground state $|G\rangle$ is populated [see Eq. (48)]. The lower and upper polaritons form a well-defined bound absorption doublet, for the transitions indicated with upper arrows in Fig. 6(b). While the dipole oscillator strength is exactly zero for the $|X\rangle$ state, making it invisible in bound absorption, its nonvanishing photonic component $\langle G|\hat{a}|X\rangle$ gives a peak in conventional absorption in Eq. (46).

The leakage photoluminescence (LPL) spectra, shown in Fig. 7, illustrates the importance of dissipative transitions of the form in Eq. (51) with $\nu \geqslant 1$. The spectrum is calculated as described in Sec. VB. If we only take into account emission events into the vibrationless ground state of the cavity (dashed

line) we obtain a photoluminescence spectra that roughly maps the conventional absorption spectra $A(\omega)$ in terms of its relative peak intensities. For example, the ratio between the LP and X peaks in conventional absorption is similar to their ratio in PL emission. However, if we include emission processes that project the system into a state with up to $\nu=1$ quantum of vibration, the emission peak near the bare molecular frequency is enhanced relative the lower polariton peak. Allowed transitions of this kind are shown in Fig. 6(b).

Leakage transitions from polariton eigenstates $|\epsilon_i\rangle$ that leave the material with $\nu \geqslant 2$ vibrational quanta are also possible, and in general contribute to the strength of the emission bands. In this work, we assume that only polaritons that are slightly higher in energy than the conventional upper polariton state are populated and can contribute to the LPL spectra. Under the assumption of uniform polariton population adopted here, photon leakage into a ground state with $\nu \geqslant 2$ quanta do not qualitatively change the emission spectra within the conventional lower and upper polariton doublet. We therefore omit those transitions from the discussion for clarity. The situation is different when a more localized polariton population is assumed [55]. In this case, emission at the lower polariton frequency can be dominated by leakage transitions with $\nu = 2$ from two-particle polariton eigenstates in the vicinity the upper polariton frequency, which is approximately two vibrational quanta above the lower polariton state for $\sqrt{N}\Omega/\omega_{\rm v}\approx 2.$

B. Molecular dimer

The dimer (N = 2) is the simplest scenario where twoparticle states need to be taken into account in order to describe the spectra. Single- and two-particle material and polariton states are described in Sec. III. We first consider the polariton dispersion for a dimer in two different Rabi coupling regimes. For relatively small Rabi frequencies $\sqrt{N}\Omega/\omega_{\rm v}\ll 1$, polaritons that arise from the lowest vibronic transition of the molecule ($\tilde{v} = 0$) have mostly single-particle character, forming the usual lower and upper polariton branches. In this Rabi coupling regime, two-particle states that originate from higher vibronic bands also lead to polariton splitting at normal incidence $(k_{\parallel} = 0)$ [46]. We show the corresponding polariton dispersion in Fig. 8(a), which displays the usual anticrossings between vibronic transitions with $\tilde{v} = 0$ and $\tilde{v} = 1$ vibrational quanta, with the vibrationless cavity photon dispersion (dashed line). As we discussed in Sec. III, the Holstein-Tavis-Cummings (HTC) model also allows the formation of the two-particle *polariton* states $|P_{\nu\tilde{\nu}'}^{\pm}, \beta\rangle$ [Eq. (24)] at normal incidence, a fact largely ignored in previous works on vibronic polaritons [44,58]. The polariton splittings associated with two-particle polaritons are smaller than for conventional (single-particle) lower and upper polariton splitting by a factor $\sqrt{1-(1/N)}$, due to the saturation nonlinearity involved in vibronic-vibrational configurations (see Fig. 2). While for large $N \gg 1$, the difference between single- and two-particle polariton splittings can be negligible, for small size systems with $N \sim 1$ [56], it may be possible to resolve the difference in polariton splittings between single-particle and multiparticle vibronic polaritons.

For Rabi frequencies closer to the critical value for the formation of the zero-energy $|X\rangle$ state, i.e., $\sqrt{N}\Omega/\omega_{\rm v}\approx 2$

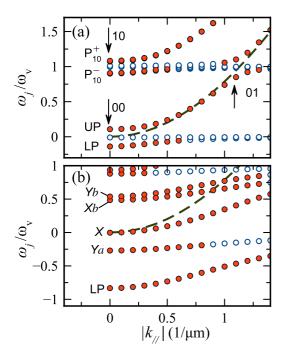


FIG. 8. Polariton dispersion for a dimer in a cavity (N=2). (a) Dispersion for Rabi coupling $\sqrt{N}\Omega=0.4\,\omega_{\rm v}$. The states ${\rm P}_{10}^\pm$ are two-particle polaritons eigenstates in this regime. Arrows indicate the location of an avoided crossing labeled by the pair of quantum numbers $(\nu\,\tilde{\nu}')$, where ν refers to the vibrational quantum number of the photon state and $\tilde{\nu}$ to the material vibronic excitation involved in polariton formation. The bare cavity dispersion is also shown (dashed line). Polariton states with at least 10% photonic character are shown with filled circles. Open circles indicate polariton states that have predominantly material character. (b) Dispersion of the lowest polariton states for Rabi coupling $\sqrt{N}\Omega=2.0\,\omega_{\rm v}$. We set $\lambda^2=1$ in both panels. $\omega_{\rm v}$ is the intramolecular vibration frequency.

(see Fig. 3), all eigenstates of the HTC model acquire a more significant contribution from two-particle material states. We show in Fig. 8(b) the polariton dispersion for this coupling regime. At normal incidence, dark vibronic polaritons of the X type (see Sec. III) are present in the middle region between the conventional lower and upper polariton branches. We label the dark vibronic polariton at zero energy by X, and the vibronic polariton that is blue shifted from the bare electronic frequency by Xb ($\omega_{Xb} \approx 0.5 \, \omega_{\rm v}$). The spectrum also features additional branches in the middle region between the conventional lower and upper polariton states. These correspond to dark vibronic polaritons of the Y type (Sec. III), and are labeled as Ya and Yb. As discussed in Sec. III D, these states are dominated by two-particle material states and can be weakly dispersive while still having a significant photon character.

In Fig. 9, we show the computed absorption and leakage photoluminescence (LPL) spectra for the bottom of the polariton branches in Fig. 8(b). The conventional and bound absorption spectra are qualitatively similar to the single molecule case (Fig. 7), with both X-type dark vibronic polaritons being visible in conventional through-mirror absorption, but only the state Xb being weakly visible in the bound absorption spectra, due to an incomplete destructive interference effect (Sec. III C). Unlike the single molecule case, the

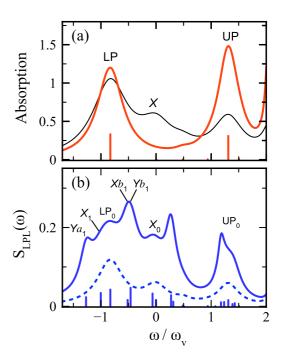


FIG. 9. Cavity absorption and emission for a dimer in a cavity (N=2). (a) Conventional absorption A=1-R-T (black line) and bound absorption spectra (red line). The lower polariton (LP) and upper polariton (UP) peaks are present in both types of absorption signals. The zero-energy dark vibronic polariton $|X\rangle$ is not present in bound absorption. (b) Leakage photoluminescence spectra (LPL) for the same parameters as in panel (a). Peak notation follows Fig. 7. Dashed and solid lines include transitions with up to $\nu=0$ and $\nu=1$ vibrational quanta, respectively, in the ground manifold. Vertical bars indicate the position and relative strength of the peak maxima. In both panels we set $\Omega=2.0\,\omega_{\rm v}$, $\kappa/\omega_{\rm v}=0.9$, $N\gamma_e/\omega_{\rm v}=0.2$, and a nonradiative decay rate $\gamma_{\rm nr}/\omega_{\rm v}=0.1$, for $\lambda^2=1$ and $\omega_c=\omega_{00}$ at normal incidence. $\omega_{\rm v}$ is the intramolecular vibration frequency.

LPL spectra for a dimer has a much richer structure when considering photon leakage transitions from dark vibronic polaritons of the Y type that leave the material with up to $\nu=1$ vibrational excitation. Such Y states are invisible in both types of absorption signals. Most notable is the appearance of multiple emission peaks in the vicinity of the conventional lower polariton peak (LP₀), which results in a broad unresolved structure for realistic linewidths. However, when considering only vibrationless photon leakage transitions ($\nu=0$), the LPL peak structure then simply resembles the conventional absorption spectra.

C. Molecular ensembles

We finally consider the spectra of large molecular ensembles in a cavity, in an effort to provide insight on the several reported features of the absorption and emission spectra [4,15,39–41] for which quasiparticle theories [36–38,42,44,58] do not offer a consistent interpretation. We compute the dispersion for a system with N=10 molecules and the spectra for N=20, which are representative values of the large N limit [47].

As we discussed for the dimer case, in the weak coupling regime, two-particle vibronic polaritons $|P_{\nu\bar{\nu}}^{\pm},\beta\rangle$ are associated

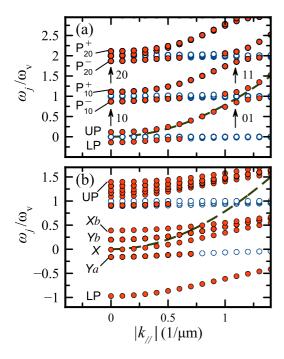


FIG. 10. Polariton dispersion for N=10 molecules in a cavity with Rabi coupling $\sqrt{N}\Omega=0.4\,\omega_{\rm v}$ at normal incidence. The states ${\rm P}^{\pm}_{\nu\bar{\nu}}$ are two-particle polaritons eigenstates in this regime. Avoided crossing are labeled by the pair of quantum numbers $(\nu\,\tilde{\nu}')$, where ν refers to the vibrational quantum number of the photon state and $\tilde{\nu}$ to the material vibronic excitation involved in polariton formation. The bare cavity dispersion is also shown (dashed line). Polariton states with at least 10% photonic character are shown with filled circles. Open circles indicate polariton states that have predominantly material character. (b) Dispersion of the lowest polariton states for Rabi coupling $\sqrt{N}\Omega=2.4\,\omega_{\rm v}$. We set $\lambda^2=1$. $\omega_{\rm v}$ is the intramolecular vibration frequency.

with Rabi splittings at frequencies greater or equal than one vibrational quanta above the conventional lower polariton splitting, as Fig. 10(a) shows. The ratio between the twoparticle Rabi splittings and the conventional lower and upper polariton splitting differs from unity by a factor of order 1/N, which is negligible for large N. The two-particle polariton branch labeled P_{10}^- in Fig. 10(a) becomes particularly important for the interpretation of the emission spectra at larger Rabi frequencies. The diabatic energy of the associated *N*-fold degenerate two-particle polariton states $|P_{1\bar{0}}^-,\beta\rangle$ [see Eq. (24)] is in the vicinity of the bare electronic frequency ($\omega_j=0$) for Rabi couplings $\sqrt{N}\Omega \approx 2\omega_{\rm v}$, and can therefore admix with single-particle diabatic material states $|\beta, \tilde{0}, 0_c\rangle$, which is also in that frequency region, forming a set of dark vibronic polaritons of the Y type for $\beta \neq \alpha_0$. These dark states are (N-1)-fold degenerate, and have a significant $\nu=1$ photonic component. Photon leakage through the mirrors would thus produce light near the conventional lower polariton frequency $\omega_{\rm LP}$, which is roughly one quantum of vibration below the bare molecular frequency for the values of $\sqrt{N\Omega}$ and λ^2 . Moreover, contributions from the two-particle diabatic polariton state labeled $P_{2\tilde{0}}^{-}$ in Fig. 10(a) would admix with the conventional (single-particle) upper polariton state for large Rabi couplings to produce a set of Y-type dark vibronic polaritons at a

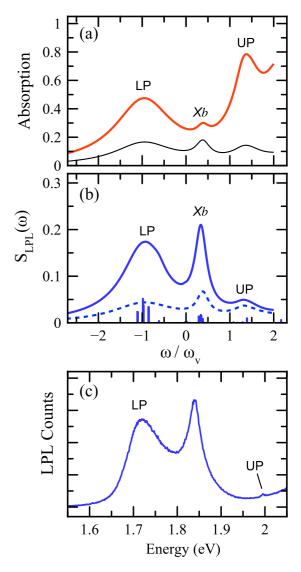


FIG. 11. Cavity absorption and emission for a microcavity with N=20 emitters. (a) Conventional absorption A=1-R-T (black line) and bound absorption spectra (red line). (b) Normal incidence LPL spectra including transitions with up to $\nu=0$ and $\nu=1$ vibrational quanta in the ground manifold, shown in dashed and solid lines, respectively. Vertical bars indicate the position and relative strength of the peak maxima. We set $\sqrt{N}\Omega=2.4\,\omega_{\rm V}, \lambda^2=1,$ $\kappa/\omega_{\rm V}=0.9,$ and $N\gamma_e/\omega_{\rm V}=3.0.$ $\omega_{\rm V}$ is the intramolecular vibration frequency. (c) Experimental LPL spectra obtained by Hobson *et al.* [4], for cyanine dye J aggregates in a low-Q microcavity (with permission). The cavity was pumped with a narrow continuous-wave laser at 2.08 eV.

frequency $\omega_j \approx \omega_v$, near the conventional upper polariton frequency. The structure of dark vibronic polaritons of the Y type is discussed in Sec. III.

As the polariton dispersion in Fig. 10(b) shows, for Rabi couplings $\sqrt{N}\Omega \approx 2\,\omega_{\rm v}$ there are several Y-type dark vibronic polaritons deriving from $|P_{2\bar{0}}^-,\beta\rangle$ that have energies near the upper polariton $(\omega_j\approx\omega_{\rm v})$. Figure 11(a) shows that dark vibronic polariton states of the Y type are invisible in both types of absorption spectra, as for the dimer case. Such Y states can nevertheless contribute to photoluminescence peak

near the conventional lower polariton frequency ($\omega_j \approx -\omega_v$), when the system is projected into a state with two vibrational quanta upon photon leakage, and also to the peak near the bare electronic frequency ($\omega_j \approx 0$) when emitting light that leaves the system with one quantum of vibration. Similarly, dark vibronic polaritons of the X and Y types near the bare electronic frequency, i.e., branches labeled Ya, X, Yb, and Xb in Fig. 10(b), also contribute to PL emission near the lower polariton frequency, when projecting the system into a state with one vibrational excitation.

Figure 10(b) also shows that there are multiple polariton branches near the upper polariton branch in the range of frequencies $\omega_i/\omega_v \approx 0.9$ –1.4. These include dark vibronic polaritons of the Y type with a photonic component having both $\nu = 1$ and $\nu = 2$ vibrational quanta. For numerical convenience, we only take into account leakage transitions that leave the system with one quantum of vibration in the computed photoluminescence spectra. Under the assumption of uniformly populated polaritons assumed here for the evaluation of the emission spectra, photon leakage transitions into states with $\nu = 2$ vibrational quanta do not qualitatively change the spectral shape. However, for a nonuniform polariton populations like the one produced by a narrow laser pulse, transitions involving v = 2 vibrational quanta in the ground manifold should be taken into account in order to obtain qualitative agreement with pump-probe experiments [55].

We show in Fig. 11(b) the calculated photoluminescence spectra (LPL) for a choice of Hamiltonian and dissipative model parameters that are representative of molecular ensembles in typical organic cavities. The results should be compared with the experimental PL spectra in Fig. 11(c), obtained by Hobson *et al.* [4] for an ensemble of cyanine dye J aggregates in a metallic microcavity at room temperature. The model calculation qualitatively reproduces the main observed emission features, with no fitting involved. The results are also consistent with other recent measurements on a different type of J aggregate (TDBC) [41]. Similar to the single-molecule and dimer cases, if we ignore emission from Y-type dark vibronic polaritons that leave the material with $\nu \geqslant 1$ vibrational quanta upon photon leakage, the relative peak strengths differ significantly from the experimentally observed ratios.

We also note the relative simplicity of the spectra for large N relative to the dimer case. The multiple emission lines near the lower polariton frequency ω_{LP} in Fig. 9, for the dimer case, merge into a single broad emission band whose peak maximum is blue-shifted relative to ω_{LP} for an ensemble. For the chosen model parameters, the shift is due to emission from the (N-1)-fold degenerate dark vibronic polariton labeled Yb in Fig. 10(b). For N=20 this state has energy $\omega_Y=0.148~\omega_v$, and can emit light with frequency $\omega_Y-\omega_v\approx-0.85~\omega_v$ upon mirror leakage, which is blue shifted from the lower polariton frequency ω_{LP} by $\delta_{LP}=0.12~\omega_v$. This value of δ_{LP} corresponds to 20 meV for a vinyl stretch ($\omega_v=180~{\rm meV}$ [51]). Shifts of this magnitude have been recently measured [41].

VII. CONCLUSIONS

In this work, we have developed a theoretical framework to describe the spectroscopy of organic microcavities based on the recently introduced Holstein-Tavis-Cummings model [33,46,49], and a Lindblad description of the dissipative dynamics of organic polaritons. The model provides a microscopic interpretation for several observed features in the absorption and emission spectra of organic microcavities in the vicinity of the spectral region associated with bare molecular transitions. Several experimental features are given a consistent interpretation here. We do this by introducing the concept of *dark vibronic polaritons*, a class of light-matter excitations that have no dipole oscillator strength, making them invisible in direct bound mode absorption [60,69], but which nevertheless have strong emission signatures in photoluminescence.

The proposed interpretation of the organic cavity spectra does not depend qualitatively on our choice of Hamiltonian parameters within the range of Rabi frequencies shown in Fig. 3, roughly defined by the Rabi coupling being twice the intramolecular vibration frequency. We refer to this range of Rabi frequencies as an intermediate coupling regime, to distinguish it from the much stronger regime described in previous work [33], where molecular vibrations become separable from the electronic and photonic degrees of freedom. In the intermediate coupling regime discussed here, vibrations, electrons, and photons are fully entangled and form two types of dark vibronic polaritons, which we call of the X and Y types. The set of X-type polaritons are dark in dipole absorption mostly due to destructive interference effects, and the set of Y-type polaritons are completely invisible in dipole absorption because they contain single- and two-particle material components that have no transition dipole moment with the absolute ground state of the system (no electronic, vibrational, or cavity excitation).

As an application of the introduced theoretical framework, we interpret the photoluminescence spectra of organic cavities. This type of observable can be divided into frequency components associated with photon leakage transitions that leave the material with $\nu \ge 0$ vibrational excitations. Therefore, within the homogeneous model considered in this work, emission near the lower polariton frequency can be due to direct radiative transitions (photon leakage) from polariton states at higher energies that leave the material with $\nu \ge 1$ vibrational quanta. Nonradiative relaxation is thus not the only mechanism that can account for the observed emission enhancements at the lower polariton frequency, under off-resonant pumping [41,70]. For large molecular ensembles in metallic cavities, we expect subpicosecond radiative relaxation to be the dominant polariton decay channel, due to a predicted size-enhanced fluorescence rate into bound modes of the nanostructure, and the short photon lifetime of low-Q microcavities [4].

In the parameter regime where dark vibronic polaritons form near of the bare molecular transition ($\sqrt{N}\Omega\approx 2\,\omega_{\rm v}$), material states that are commonly considered to be uncoupled from the cavity field (dark excitons) can borrow an appreciable photonic component from higher energy two-particle diabatic vibronic polaritons. In other words, there are no collective material states that remain uncoupled from the cavity field. Eventually, as the Rabi coupling increases far beyond the threshold for polaron decoupling [33], the cavity spectra is expected to simplify. The study of the spectral changes in absorption and emission as the cavity transitions from the regime of dark vibronic polariton formation to the polaron decoupling regime is currently underway.

Possible experimental tests of the predicted photophysics of organic microcavities can include a comparison between polariton photoluminescence into bound modes of the nanostructure versus the conventional leakage photoluminescence into free space. If the external pump field is only slightly blue detuned relative to the lower polariton frequency, then dark vibronic polaritons are not populated and their effects on emission can be suppressed [55]. We find that the ratio between the vibrationless emission peak from (0-0) and the first vibronic sideband (0-1), associated with a transition from the lower polariton into the ground electronic manifold with one quantum of vibration, is different when measured via leakage photoluminescence in comparison with bound photoluminescence. Interestingly, only the bound mode 0-0/0-1 ratio is indicative of cavity-induced coherence length in the ensemble [46], resembling the behavior of molecular aggregates in free space [71].

In summary, we have demonstrated that a simple homogeneous treatment of the system with purely radiative relaxation can qualitatively describe several observed features of the spectroscopy of organic microcavities. More quantitative comparisons would require further extensions of the model, in order to account for long-range electrostatic coupling between emitters, strong energetic disorder, multimode cavity couplings, and more general radiative and nonradiative reservoirs. The model can be further extended to describe microcavities in the ultrastrong coupling regime [11,12,16] having arbitrary mode dispersion. Our work thus paves the way for the development of novel nonlinear optical devices [21,27,29,30], chemical reactors [31,33], and optoelectronic devices [23–26] that can be enhanced by quantum optics.

ACKNOWLEDGMENTS

We thank Bill Barnes for providing the photoluminescence data from Ref. [4], Marina Litinskaya for technical discussions, and Jonathan Keeling for comments. F. Herrera is supported by CONICYT through PAI No. 79140030 and Fondecyt Iniciación No. 11140158. F. C. Spano is supported by the NSF, Grant No. DMR-1505437.

APPENDIX A: SYMMETRY OF THE HTC MODEL

Here we prove that

$$e^{-i\hat{S}}\hat{H}_{LM}e^{i\hat{S}} = \hat{H}_{LM}. \tag{A1}$$

In order to do so, it is sufficient to show that the commutator $[\hat{S}, \hat{H}_{LM}]$ vanishes. Using the definitions in Eqs. (2) and (3), we can write this commutator as

$$\begin{split} [\hat{S}, \hat{H}_{LM}] \\ &= \frac{1}{2} \sum_{\nu \nu'} [(-1)^{-\nu} \Omega_{\nu \tilde{\nu}'} - (-1)^{\nu'} \Omega_{\tilde{\nu} \nu'}] |e \, \tilde{\nu} \, 0_c \rangle \langle e \, \tilde{\nu}' \, 0_c | \\ &+ \frac{1}{2} \sum_{\nu \nu'} [(-1)^{-\nu'} \Omega_{\tilde{\nu}' \nu} - (-1)^{\nu} \Omega_{\nu' \tilde{\nu}}] |g \, \nu' \, 1_c \rangle \langle g \, \nu \, 1_c |. \end{split}$$
(A2)

We use the following symmetry property of Frank-Condon factors under the exchange of vibrational indices [59]

$$\langle \nu' | \tilde{\nu} \rangle = (-1)^{\nu - \nu'} \langle \nu | \tilde{\nu}' \rangle \tag{A3}$$

to show that the square brackets in the first and second lines of Eq. (A2) can be rewritten to give

$$(-1)^{-\nu}\Omega_{\nu\tilde{\nu}'} - (-1)^{\nu'}\Omega_{\tilde{\nu}\nu'} = (-1)^{\nu}[\Omega_{\nu\tilde{\nu}'} - \Omega_{\tilde{\nu}'\nu}] = 0 \quad (A4)$$

and

$$(-1)^{-\nu'}\Omega_{\tilde{\nu}'\nu} - (-1)^{\nu}\Omega_{\nu'\tilde{\nu}} = (-1)^{\nu'}[\Omega_{\tilde{\nu}'\nu} - \Omega_{\nu\tilde{\nu}'}] = 0, \ \ (A5)$$

which proves the desired commutation property.

APPENDIX B: PROOF THAT $\langle G | \hat{\mu} | X \rangle = 0$

In this section we prove that a zero-energy vibronic polariton eigenstate of the HTC Hamiltonian $\hat{\mathcal{H}}$ [Eq. (1)], in a frame rotating at the cavity frequency ω_c , has no dipole oscillator strength for transitions from the absolute ground state of the cavity $|G\rangle \equiv |g_1 \, 0_1, g_2 \, 0_2, \dots, g_N \, 0_N\rangle |0_c\rangle$.

We write the transition dipole operator as $\hat{\mu} = \hat{\mu}^{(+)} + \hat{\mu}^{(-)}$, where $\hat{\mu}^{(+)} = \mu \sum_n |g_n\rangle\langle e_n|$ and $\hat{\mu}^{(-)} = [\hat{\mu}^{(+)}]^{\dagger}$, with μ being the single-particle transition dipole moment. Denoting as $|X\rangle$ the vibronic polariton eigenstate with zero eigenvalue in the cavity frame, we have

$$\hat{\mathcal{H}}|X\rangle = (\hat{H}_{M} + \hat{H}_{LM})|X\rangle = 0, \tag{B1}$$

where in the second line we express the HTC Hamiltonian as a sum of a material term $\hat{H}_{\rm M}$ and a light-matter coupling term $\hat{H}_{\rm LM}$. The free cavity term $\omega_c \hat{a}^{\dagger} \hat{a}$ is eliminated by transforming to a frame rotating at the cavity frequency ω_c [59].

The material (Holstein) Hamiltonian can be written as

$$\hat{H}_{\rm M} = \sum_{n} \hat{h}_{\rm vib}^{n} + \hat{h}_{\rm vib}^{n}(\lambda) |e_{n}\rangle\langle e_{n}|, \tag{B2}$$

with \hat{h}^n_{vib} being the reference (unshifted) vibrational Hamiltonian and $\hat{h}^n_{\text{vib}}(\lambda)$ being the displaced vibrational Hamiltonian in the excited electronic state. Therefore, left-multiplying Eq. (B2) by the state $\langle G|\hat{a}$ we obtain $\langle G|\hat{a}\hat{H}_{\text{M}}=\langle G|\hat{a}(\sum_n\hat{h}^n_{\text{vib}})=0$, since there are no vibrational excitations in $|G\rangle$. When we now left-multiply Eq. (B1) by $\langle G|\hat{a}$, the light-matter term gives

$$\langle g_1 \, 0_1, g_2 \, 0_2, \dots, g_N \, 0_N | \langle 1_c | \sum_n \{ |g_n\rangle \langle e_n | \hat{a}^{\dagger}$$

$$+ |e_n\rangle \langle g_n | \hat{a} \} | X \rangle = 0.$$
(B3)

Only the first term in the curly bracket contributes to the lefthand side of this equality, giving

$$\langle G|\hat{\mu}^{(+)}|X\rangle = 0. \tag{B4}$$

This expression gives the desired result $\langle G|\hat{\mu}|X\rangle=0$, by noting that $\langle G|\hat{\mu}^{(-)}=0$.

APPENDIX C: INPUT-OUTPUT RELATIONS

We review here the input-output theory for transmission and reflection spectra of a two-sided planar cavity. We follow the so-called quasimode approximation, in which orthogonal degrees of freedom inside and outside the cavity are defined, these being weakly coupled to each other via finite transmission through the cavity mirrors [61,72]. The formalism is an alternative to the field quantization approach based on the classical Green's function of the problem [73]. We follow the Schrodinger picture approach from Carmichael *et al.* [61], which differs the Heisenberg picture approach from Collet and Gardiner [74,75] in that no time-reversed solutions are invoked.

The dynamics of an empty cavity coupled to the electromagnetic reservoirs at each external side of the cavity mirrors is given by the Hamiltonian $\hat{H} = \hat{H}_S + \hat{H}_R + \hat{H}_{SR}$, where

$$\hat{H}_{S} = \sum_{\beta} \omega_{\beta} \, \hat{a}_{\beta}^{\dagger} \hat{a}_{\beta},$$

$$\hat{H}_{R} = \sum_{i\beta} \int_{0}^{\infty} d\omega \, \omega [\hat{l}_{i\beta}^{\dagger}(\omega) \hat{l}_{i\beta}(\omega) + \hat{r}_{i\beta}^{\dagger}(\omega) \hat{r}_{i\beta}(\omega)],$$

$$\hat{H}_{SR} = \sum_{i\beta} \int_{0}^{\infty} d\omega \, \kappa_{i}^{*}(\omega) \, \hat{a}_{\beta} [\hat{l}_{i\beta}^{\dagger}(\omega) + \hat{r}_{i\beta}^{\dagger}(\omega)] + \text{H.c.},$$
(C1)

where the operators $\hat{l}_{i\beta}(\omega)$ and $\hat{r}_{i\beta}(\omega)$ are continuous reservoir field operators that annihilate a free-space photon with frequency ω and in-plane wave vector $\boldsymbol{\beta}$ propagating to the left and to the right relative to the cavity axis, on regions i=1 (left side of cavity) and region i=2 (right side). We implicitly assumed that all fields involved have transverse electric (TE) polarization $\hat{\mathbf{e}}_{\beta}$ and only the lowest TE cavity mode is taken into account. We have also used the fact that transmission through the cavity mirror preserves the in-plane wave vector $\boldsymbol{\beta}$ of the field away from the mirror edges. Since the cavity length L is subwavelength, higher order TE modes with are far detuned from the electronic transition frequencies of interest. The system-reservoir couplings $\kappa_i(\omega)$ determine the cavity decay rate at each mirror, as we show below. The reservoir operators satisfy the equal-time commutation relations of the form

$$\begin{split} [\hat{l}_{i\beta}(\omega), \hat{l}^{\dagger}_{k\beta'}(\omega')] &= [\hat{r}_{i\beta}(\omega), \hat{r}^{\dagger}_{k\beta'}(\omega')] = \delta_{ik}\delta(\omega - \omega'), \\ [\hat{l}_{i\beta}, \hat{r}^{\dagger}_{k\beta'}] &= [\hat{a}_{\beta}, \hat{r}^{\dagger}_{k\beta'}] = [\hat{a}_{\beta}, \hat{l}^{\dagger}_{k\beta'}] = 0. \end{split}$$
(C2)

Cavity and reservoir operators evaluated at different times do not necessarily commute.

We can avoid referring to the electric field normalization outside the cavity by defining the electric field operator in units of photon flux for *i*th region $\hat{\mathcal{E}}_i^{(+)}(\mathbf{x},t) = \sum_{\beta} \mathrm{e}^{i\beta \cdot \mathbf{x}_{\parallel}} \hat{\mathcal{E}}_{i\beta}(z,t)$, with

$$\sqrt{2\pi} \,\hat{\mathcal{E}}_{i\beta}^{(+)}(z,t) = \int_0^\infty d\omega \,\hat{l}_{i\beta}(\omega,t) e^{-i\omega\zeta_i(z)/c} + \int_0^\infty d\omega \,\hat{r}_{i\beta}(\omega,t) e^{i\omega\zeta_i(z)/c}, \quad (C3)$$

where $\zeta_1(z) \equiv z \cos \theta_1 < 0$ is the projected wavefront distance relative to the z axis (cavity axis) with θ_1 being the incidence angle in region 1. For region 2 we have the scaled position $\zeta_2(z) \equiv (z - L) \cos \theta_2 > 0$, where θ_2 is the incidence angle relative to the cavity axis. In what follows, we evaluate the frequency integrals by writing $\omega = \omega_\beta + \Delta$, where Δ is the detuning from the cavity resonance frequency ω_β . The

resulting expressions are simplified when written in terms of rotating-frame operators defined as $\tilde{A}(t) \equiv \hat{A}(t)e^{i\omega_{\beta}t}$.

The Heisenberg equations of motion for the rotating-frame operators $\tilde{l}_{i\beta}(\Delta,t)$ and $\tilde{r}_{i\beta}(\Delta,t)$ in each region can be formally solved to read

$$\tilde{l}_{i\beta}(t) = \tilde{l}_{i\beta}(0)e^{-i\Delta t} - i\kappa_{i}^{*}(\Delta) \int_{0}^{t} dt' \ e^{-i\Delta(t-t')} \tilde{a}_{\beta}(t'),$$

$$\tilde{r}_{i\beta}(t) = \tilde{r}_{i\beta}(0)e^{-i\Delta t} - i\kappa_{i}^{*}(\Delta) \int_{0}^{t} dt' \ e^{-i\Delta(t-t')} \tilde{a}_{\beta}(t'), \quad (C4)$$

where we have omitted for simplicity the frequency dependence of the reservoir operators. These formal solutions are then inserted into the rotating-frame version of Eq. (C3) to obtain a field of the form

$$\hat{\mathcal{E}}_{i\beta}^{(+)} = \hat{\mathcal{E}}_{i\beta L}^{(+)} + \hat{\mathcal{E}}_{i\beta R}^{(+)} + \hat{\mathcal{E}}_{i\beta S}^{(+)},\tag{C5}$$

where

$$\hat{\mathcal{E}}_{i\beta L}^{(+)}(z,t) = e^{-i\omega_{\beta}(t+\zeta_{i}/c)} \int \frac{d\Delta}{\sqrt{2\pi}} \,\tilde{l}_{i\beta}(\Delta,0) e^{-i\Delta(t+\zeta_{i}/c)}, \quad (C6)$$

and

$$\hat{\mathcal{E}}_{i\beta R}^{(+)}(z,t) = e^{-i\omega_{\beta}(t-\zeta_{i}/c)} \int \frac{d\Delta}{\sqrt{2\pi}} \,\tilde{r}_{i\beta}(\Delta,0) e^{-i\Delta(t-\zeta_{i}/c)} \quad (C7)$$

are free fields propagating to the left and to the right along the z axis, respectively. As expected for free fields, these expressions give $[\hat{\mathcal{E}}^{(+)}_{i\beta L}(z,t),\hat{\mathcal{E}}^{(-)}_{i\beta L}(z,t')] = [\hat{\mathcal{E}}^{(+)}_{i\beta R}(z,t),\hat{\mathcal{E}}^{(-)}_{i\beta R}(z,t')] = \delta(t-t')$. The reservoir operators $\tilde{l}_{i\beta}(\Delta)$ and $\tilde{r}_{i\beta}(\Delta)$ evaluated at t=0, become input field operators in the formalism by Collet and Gardiner [74]. The total field $\hat{\mathcal{E}}^{(+)}_{i\beta}$ also has a source contribution that depends on the intracavity field and can be written as

$$\sqrt{2\pi} \,\hat{\mathcal{E}}_{i\beta S}^{(+)}(z,t)
= -ie^{-i\omega_{\beta}(t+\zeta_{i}/c)} \int d\Delta \,\kappa_{i}^{*}(\Delta) \int_{0}^{t} dt' \,e^{-i\Delta(t-t'+\zeta_{i}/c)} \tilde{a}_{\beta}(t')
-ie^{-i\omega_{\beta}(t-\zeta_{i}/c)} \int d\Delta \,\kappa_{i}^{*}(\Delta) \int_{0}^{t} dt' \,e^{-i\Delta(t-t'-\zeta_{i}/c)} \tilde{a}_{\beta}(t').$$
(C8)

Causality ensures that either on the left or right side of the cavity, only one term in Eq. (C8) contributes to the source field. Physically, it is not possible for a right-propagating field far to the left cavity mirror $(\zeta_1 \to -\infty)$, for example, to depend on the intracavity field operator \tilde{a}_{β} because it has yet to reach the mirror. Therefore its contribution to the source field $\hat{\mathcal{E}}^{(+)}_{i\beta S}$ must vanish. The left-propagating contribution at the same distant location can, however, depend on the intracavity field after reflection at the left cavity mirror. Such causal behavior is obtained in a simple form by assuming a frequency-independent coupling of the form $\kappa_i(\omega) \approx \kappa_i(\omega_{\beta})$ over the frequency range $\omega_{\beta} - \delta_c < \omega < \omega_{\beta} + \delta_c$, where δ_c is a cutoff frequency, which gives $\kappa_i(\Delta) = \kappa_i(0)$ in the rotating frame of the cavity mode. The frequency integrals in Eq. (C8) can be easily evaluated by setting $\delta_c \to \infty$. The source field

in region 1 ($\zeta_1 < 0$) thus reads

$$\begin{split} \hat{\mathcal{E}}_{1\beta S}^{(+)}(z,t) &= -i\sqrt{2\pi} \,\,\kappa_1^*(0) \\ &\times \left[e^{-i\omega_\beta(t+\zeta_1/c)} \int_0^t dt' \tilde{a}_\beta(t') \delta(t+\zeta_1/c-t') \right. \\ &+ e^{-i\omega_\beta(t-\zeta_1/c)} \int_0^t dt' \tilde{a}_\beta(t') \delta(t-\zeta_1/c-t') \right]. \end{split}$$
(C9)

The second time integration (right-propagating wave) vanishes because the peak of the δ function lies outside the integration range (0,t) for $\zeta_1 \leq 0$. Only the left-propagating contribution survives, giving the source field

$$\hat{\mathcal{E}}_{1\beta S}^{(+)}(z,t) = -ie^{-i\omega_{\beta}(t+\zeta_{1}/c)}\sqrt{2\pi} \,\,\kappa_{1}^{*}(0)\,\tilde{a}_{\beta}(t-|\zeta_{1}|/c), \tag{C10}$$

which depends on the intracavity field evaluated at the retarded time $t-|\zeta_1|/c$, as expected from causality. We made the change of variable $\tau=t+\zeta_1/c-t'$ in evaluating the time integral. The source contribution in region 2 ($\zeta_2\geqslant 0$) can be obtained in an analogous way to give

$$\hat{\mathcal{E}}_{2\beta S}^{(+)}(z,t) = -ie^{-i\omega_{\beta}(t-\zeta_{2}/c)}\sqrt{2\pi} \,\kappa_{2}^{*}(0)\,\tilde{a}_{\beta}(t-\zeta_{2}/c). \quad (C11)$$

The coupling constants $\kappa_i(0)$ evaluated at the cavity resonance frequency ω_{β} are related to the damping rates γ_i that determine the cavity linewidth [61]. Starting from the Heisenberg equation of motion for the slowly-varying amplitude

$$\frac{d}{dt}\tilde{a}_{\beta} = -i\sum_{i} \int_{-\infty}^{\infty} d\Delta \,\kappa_{i}(\Delta)[\hat{l}_{i\beta}(\Delta,t) + \hat{r}_{i\beta}(\Delta,t)], \quad (C12)$$

after inserting the formal solutions from Eq. (C4), we arrive at the Langevin equation

$$\frac{d}{dt}\tilde{a}_{\beta} = -\int_{0}^{t} dt' \left[K_{1}(t - t') + K_{2}(t - t') \right] \tilde{a}_{\beta}(t')
+ \hat{L}_{1\beta}(t) + \hat{R}_{1\beta}(t) + \hat{L}_{2\beta}(t) + \hat{R}_{1\beta}(t), \quad (C13)$$

with dissipation kernel

$$K_i(t - t') = \int_{-\infty}^{\infty} d\Delta |\kappa_i(\Delta)|^2 e^{-i\Delta(t - t')}, \quad (C14)$$

and source operators

$$\hat{L}_{i\beta}(t) = -i \int_{-\infty}^{\infty} d\Delta \,\kappa_i(\Delta) \tilde{l}_{i\beta}(\Delta, 0) e^{-i\Delta t} \qquad (C15)$$

$$\hat{R}_{i\beta}(t) = -i \int_{-\infty}^{\infty} d\Delta \,\kappa_i(\Delta) \tilde{r}_{i\beta}(\Delta, 0) e^{-i\Delta t}. \quad (C16)$$

These are determined by the input reservoir operators $\tilde{l}_{i\beta}(\Delta)$ and $\tilde{r}_{i\beta}(\Delta)$ at each side of the cavity. In the Markovian approximation for the cavity-mirror coupling, the dissipation kernels become $K_i(t-t') = (2\pi)|\kappa_i(0)|^2\delta(t-t')$. Setting

$$\gamma_i = 2\pi |\kappa_i(0)|^2, \tag{C17}$$

and using the relation $\int_0^t d\tau f(\tau)\delta(\tau) = f(0)/2$ to integrate the time kernels, gives a time-local equation of motion

$$\frac{d}{dt}\tilde{a}_{\beta}(t) = -(\gamma/2)\,\tilde{a}_{\beta}(t) + \sqrt{\gamma_1}\,\tilde{F}_{1\beta}(t) + \sqrt{\gamma_2}\,\tilde{F}_{2\beta}(t),\tag{C18}$$

where $\gamma = (\gamma_1 + \gamma_2)$ is the cavity decay rate, and the Langevin noise operators are given by

$$\tilde{F}_{i\beta}(t) = -\frac{i}{\sqrt{2\pi}} e^{i\phi_i} \int d\Delta \left[\tilde{l}_{i\beta}(\Delta, 0) + \tilde{r}_{i\beta}(\Delta, 0) \right] e^{-i\Delta t},$$
(C19)

where we have defined the phase ϕ_i as $\kappa_i(0) = |\kappa_i(0)|e^{i\phi_i}$. It is well known that the Langevin equation in Eq. (C18) can be rewritten for coherent input fields as the Lindblad quantum master equation [61]

$$\dot{\hat{\rho}} = -i[\hat{H}_S, \hat{\rho}] + \gamma \left(\hat{a}_{\beta} \hat{\rho} \hat{a}_{\beta}^{\dagger} - \frac{1}{2} \{\hat{a}_{\beta}^{\dagger} \hat{a}_{\beta}, \hat{\rho}\}\right), \tag{C20}$$

where $\hat{\rho}$ is intracavity photon reduced density matrix and the curly brackets denote an anticommutator. The Langevin noise operators $F_{i\beta}(t)$ are represented by a near-resonant driving Hamiltonian term, such that the intracavity Hamiltonian reads

$$\hat{H}_S = \omega_{\beta} \hat{a}_{\beta}^{\dagger} \hat{a}_{\beta} + \mathcal{E}_1^* \hat{a}_{\beta} e^{-i\Delta_{\beta}t} + \mathcal{E}_1 \hat{a}_{\beta}^{\dagger} e^{i\Delta_{\beta}t}, \quad (C21)$$

where $\mathcal{E}_1 = \sqrt{\gamma_1}\beta_1$ is the driving strength corresponding to an input coherent state with complex amplitude β_1 on mirror 1, detuned from the cavity resonance by Δ_{β} , assuming driving on region 1 only.

Transmission and reflection experiments measure the spectrum of the external electric field $\hat{\mathcal{E}}_i^{(+)}(\mathbf{x},t)$ for a given in-plane momentum $\boldsymbol{\beta}$ at a fixed position $\mathbf{x} = \mathbf{x}_i$. For driving on region 1, the reflection spectra $R(\omega)$ is determined by the Fourier transform of the normalized first-order correlation function [77]

$$g_1^{(1)}(t,\tau) = \frac{\langle \hat{\mathcal{E}}_{1\beta}^{(-)}(t+\tau)\hat{\mathcal{E}}_{1\beta}^{(+)}(t)\rangle}{\langle \hat{\mathcal{E}}_{1\beta}^{(-)}(t)\hat{\mathcal{E}}_{1\beta}^{(+)}(t)\rangle}.$$
 (C22)

The transmission spectra $T(\omega)$ would be proportional to the Fourier transform of the field correlation function $\langle \hat{\mathcal{E}}_{2\beta}^{(-)}(t+\tau)\hat{\mathcal{E}}_{2\beta}^{(-)}(t)\rangle$, corresponding to region 2.

The field expansion introduced in Eq. (C5) shows that in general the output spectrum [either $R(\omega)$ of $T(\omega)$] depends on the correlations between the reservoir and intracavity field operators. However, these can be neglected at optical frequencies for thermal reservoirs [61], giving the stationary correlation function ($\tau > 0$)

$$g_{i}^{(1)}(t,\tau) \approx \frac{\left[\langle \hat{\mathcal{E}}_{i\beta L}^{(-)}(t+\tau)\hat{\mathcal{E}}_{i\beta L}^{(+)}(t)\rangle + \langle \hat{\mathcal{E}}_{i\beta R}^{(-)}(t+\tau)\hat{\mathcal{E}}_{i\beta R}^{(+)}(t)\rangle\right]}{\langle \hat{\mathcal{E}}_{i\beta}^{(-)}(t)\hat{\mathcal{E}}_{i\beta}^{(+)}(t)\rangle} + \frac{\pi \gamma_{i} \langle \tilde{a}_{\beta}^{\dagger}(t+\tau)\tilde{a}_{\beta}(t)\rangle}{\langle \hat{\mathcal{E}}_{i\beta}^{(-)}(t)\hat{\mathcal{E}}_{i\beta}^{(+)}(t)\rangle}. \tag{C23}$$

The steady-state spectrum is obtained by taking the limit $t \to \infty$ in Eq. (C22). Therefore, once the input field spectrum is known (driving laser), the stationary transmission and reflection spectra are completely determined by the intracavity

two-time correlation function $\langle \tilde{a}_{\beta}^{\dagger}(t+\tau)\tilde{a}_{\beta}(t)\rangle$, which can be evaluated from the Lindblad master equation or Langevin equation for the system evolution, together with the quantum regression theorem [61].

1. Transmission and reflection

Before discussing light absorption by a molecular medium embedded in the cavity, let us consider a two-mirror cavity driven by a stationary coherent input field with (complex) amplitude $\langle \hat{F}_{1\beta} \rangle \neq 0$ on region 1, i.e., $\langle \hat{F}_{2\beta} \rangle = 0$ in Eq. (C18). The steady-state amplitude of the intracavity field is thus

$$\langle a_{\beta} \rangle_{\rm ss} = -\frac{2\sqrt{\gamma_1}}{\gamma} \langle \hat{F}_{1\beta} \rangle.$$
 (C24)

From Eqs. (C6), (C7), (C10), and (C19), we can write the electric field flux amplitude at the reflecting mirror ($\zeta_1 = 0$) as

$$|\langle \hat{\mathcal{E}}_{1\beta}^{(+)} \rangle| = |\langle \hat{F}_{1\beta} \rangle| \left(1 - \frac{2\gamma_1}{\gamma} \right) = |\langle \hat{F}_{1\beta} \rangle| \left(\frac{\gamma_2 - \gamma_1}{\gamma_2 + \gamma_1} \right). \quad (C25)$$

A similar calculation for the electric field amplitude at the transmitting mirror ($\zeta_2 = 0$) gives

$$|\langle \hat{\mathcal{E}}_{2\beta}^{(+)} \rangle| = |\langle \hat{F}_{1\beta} \rangle| \frac{\sqrt{\gamma_1 \gamma_2}}{\gamma_1 + \gamma_2}. \tag{C26}$$

These expressions simply state the fact that for identical mirrors ($\gamma_1 = \gamma_2$), the reflected field vanishes and the cavity acts as a perfect transmission filter, which is known from classical interferometry [76]. Since there is no absorption in the cavity, conservation of photon flux can be stated as

$$|\langle \hat{\mathcal{E}}_{1\beta}^{(+)} \rangle|^2 + |\langle \hat{\mathcal{E}}_{2\beta}^{(+)} \rangle|^2 = |\langle \hat{F}_{1\beta} \rangle|^2. \tag{C27}$$

Normalizing the reflected and transmitted fluxes by the input photon flux results in the identity

$$R + T = 1$$
,

where R and T are the reflectivity and transmittivity of the cavity at a given input frequency.

2. Cavity absorption

Let us now consider a molecular medium embedded in a two-side cavity. The interaction between the molecular transition dipole moment operator of the *n*th molecule in the ensemble $\hat{\mu}_n$ and the local electric field operator $\hat{\mathcal{E}}(\mathbf{x}_n)$ is represented, ignoring a global phase, by the interaction term

$$\hat{H}_I = \sum_n \hat{\mu}_n \,\hat{\mathcal{E}}(\mathbf{x}_n) = \sum_n \hat{\mu}_n^{(-)} \,\hat{\mathcal{E}}^{(+)}(\mathbf{x}_n) + \text{H.c.}, \quad (C28)$$

where in the second equality we use $\hat{\mu} = \hat{\mu}^{(+)} + \hat{\mu}^{(-)}$ and adopted the rotating-wave approximation (RWA) [77]. The local electric field at the molecular position \mathbf{x}_n is given by superposition of multiple field modes of the microcavity. The field modes whose in-plane wave vector $\boldsymbol{\beta}$ does not exceed the cutoff for total internal reflection are able to leak out of the nanostructure through the mirrors. These so-called *radiative* modes are involved in transmission and reflection measurements [4]. The dynamics of the radiative modes is determined by the field operator $\hat{a}_{\boldsymbol{\beta}}$, which satisfies Eq. (C18) for an empty cavity.

For those field modes whose in-plane wave vector exceed the cutoff for total internal reflection, photons are unable to leak through the mirrors and remain bound to the intracavity space. Bound modes are mostly confined to the bulk of the dielectric medium or at the mirror-dielectric interface and represent a decay channel for molecular electronic transitions that can reduce the efficiency of light-emitting devices [60]. The degree in which a bound mode is either bulk or a surface mode depends on the field polarization and the distance between the mirrors [65]. We use the operator $\hat{b}_{\beta'}(\omega)$ to represent a bound mode with in-plane wave vector β' , and write the local intracavity (positive frequency) electric field as the superposition

$$\hat{\mathcal{E}}^{(+)}(\mathbf{x}_n) = \hat{\mathcal{E}}_a^{(+)}(\mathbf{x}_n) + \hat{\mathcal{E}}_b^{(+)}(\mathbf{x}_n),$$

where $\hat{\mathcal{E}}_a^{(+)}(\mathbf{x}_n)$ is the contribution to the electric field from radiative modes, and $\hat{\mathcal{E}}_b^{(+)}(\mathbf{x}_n)$ the contribution from bound modes. We treat radiative and bound modes differently in our model. We include only the radiative modes as part of the Holstein-Tavis-Cummings (HTC) Hamiltonian, which reads

$$\hat{\mathcal{H}} = \hat{H}_{C} + \hat{H}_{M} + \hat{V}_{a}, \tag{C29}$$

where \hat{H}_C is the free cavity Hamiltonian from Eq. (C1), \hat{H}_M is the Holstein Hamiltonian involving electronic and vibrational degrees of freedom of the material, and $\hat{V}_a = \sum_n [\hat{\mu}_n^{(-)} \hat{\mathcal{E}}_a^{(+)}(\mathbf{x}_n) + \text{H.c.}]$ is the cavity-matter coupling. The bound modes are considered as a zero-temperature electromagnetic reservoir that induces dissipation of the molecular dipoles via spontaneous emission. Expanding the bound electric field as

$$\sqrt{2\pi}\,\hat{\mathcal{E}}_b^{(+)}(\mathbf{x}) = \sum_{\boldsymbol{\beta}'} \int_0^\infty d\omega\,\hat{b}_{\boldsymbol{\beta}'}(\omega) e^{i\,\boldsymbol{\beta}'\cdot\mathbf{x}},\tag{C30}$$

gives an effective system-reservoir coupling Hamiltonian of the form

$$\hat{H}_{SR} = \sum_{n} \sum_{\beta'} \int_{0}^{\infty} d\omega \, g(\omega) \, \hat{\sigma}_{n}^{-} \, \hat{b}_{\beta'}(\omega) \, e^{i\beta' \cdot \mathbf{x}_{n}} + \text{H.c.},$$
(C3)

where $\hat{\sigma}_n^- = \hat{\mu}_n^{(+)}/\mu$ is the electronic transition operator of the nth molecule, μ is the transition dipole moment, and $g(\omega)$ is a coupling function. It is well known [61,63,77] that this system-reservoir interaction in the Born-Markov approximation gives a Lindblad quantum master equation for the system density matrix $\hat{\rho}$ of the form

$$\frac{d}{dt}\hat{\rho}(t) = -i[\hat{\mathcal{H}}, \hat{\rho}(t)] + \mathcal{L}_a[\hat{\rho}(t)] + \mathcal{L}_{\mu}[\hat{\rho}(t)], \quad (C32)$$

where \mathcal{H} is the HTC Hamiltonian in Eq. (C29), $\mathcal{L}_a[\hat{\rho}(t)]$ is the cavity photon Lindblad dissipator given by the second term in Eq. (C20), and $\mathcal{L}_{\mu}[\hat{\rho}(t)]$ is the dissipator associated with dipole radiative decay into bound modes, which can be written as

$$\mathcal{L}_{\mu}[\hat{\rho}(t)] = \sum_{n} \gamma_n \left(\hat{\sigma}_n^- \hat{\rho}(t) \hat{\sigma}_n^+ - \frac{1}{2} \{ \hat{\sigma}_n^+ \hat{\sigma}_n^-, \hat{\rho}(t) \} \right), \quad (C33)$$

where γ_n is single-emitter decay rate γ_n .

We can follow a derivation to the one described above for an empty cavity and formally solve the Heisenberg equation of motion for the slowly varying variable $\tilde{b}_{\beta'}(\Delta,t)$, where Δ

is a small detuning of the bound mode frequency $\omega_{\beta'}$ from the empty cavity frequency ω_{β} . We use this formal solution to write the bound electric field amplitude as

$$\hat{\mathcal{E}}_{b}^{(+)}(\mathbf{x},t) = -i \sum_{n,\beta'} e^{i[\boldsymbol{\beta}' \cdot (\mathbf{x} - \mathbf{x}_{n}) - \omega_{\boldsymbol{\beta}'} t]}$$

$$\times \int \frac{d\Delta}{\sqrt{2\pi}} g^{*}(\Delta) \int_{0}^{t} dt' e^{-i\Delta(t-t')} \tilde{\sigma}_{n}^{-}(t').$$
(C34)

We neglect the free field contribution to $\hat{\mathcal{E}}_b^{(+)}$ because its mean amplitude vanishes for a zero-temperature electromagnetic reservoir, i.e., $\langle \tilde{b}_{\beta'}(\Delta,0) \rangle = 0$, and its contribution to the field second moments is separable [61]. The bound field is thus determined by a sum over dipole sources, and its dynamics is given by the evolution of the slowly varying transition operator $\tilde{J}_n^{(+)}(t)$. Assuming $g(\Delta) \approx g(0)$ and that $|\mathbf{x} - \mathbf{x}_n| \approx |\mathbf{x}|$ in the far field, we obtain

$$\hat{\mathcal{E}}_b^{(+)}(\mathbf{x},t) = -i\sqrt{2\pi} g^*(0) \sum_{\boldsymbol{\beta}'} \sum_n \tilde{\sigma}_n^-(t - |\mathbf{x}|/c) e^{-i(\omega_{\boldsymbol{\beta}'}t - \boldsymbol{\beta}' \cdot \mathbf{x})}.$$
(C35)

The fluorescence spectrum associated with spontaneously emitted light into bound modes by the molecules in the ensemble is thus determined by the Fourier transform of the first-order correlation function

$$g_b^{(1)}(t,\tau) = \frac{\langle \hat{\mathcal{E}}_b^{(-)}(\mathbf{x}, t + \tau) \hat{\mathcal{E}}_b^{(+)}(\mathbf{x}, t) \rangle}{\langle \hat{\mathcal{E}}_b^{(-)}(\mathbf{x}, t) \hat{\mathcal{E}}_b^{(+)}(\mathbf{x}, t) \rangle},$$
(C36)

which can be evaluated from the evolution of the dipole coherence $\sum_n \langle \sigma_n^-(t) \rangle$, together with the quantum regression theorem [61]. For simplicity, we assume that two-point dipole correlations of the form $\langle \sigma_n^+(\tau) \sigma_m^-(0) \rangle$ are negligibly small for the time scales of interest, which is consistent with the local decay approximation assumed in Eq. (C33).

We finally relate the adopted cavity QED approach to cavity emission [61] with the usual definition of cavity absorption $A(\omega)$ in semiconductor microcavities. The microcavity is assumed to be driven with a continuous wave coherent field of frequency ω_p , on the external side of one of the mirrors (region 1). For simplicity of notation, we assume driving at normal incidence ($\beta = 0$). The photon flux (in Hz) of the driving field given by $|\langle \hat{F}_1 \rangle|^2$. In the absence of dipole decay, radiative or nonradiative, the reflected and transmitted photon fluxes, $|\langle \hat{\mathcal{E}}_1^{(+)} \rangle|^2$ and $|\langle \hat{\mathcal{E}}_2^{(+)} \rangle|^2$, respectively, should satisfy Eq. (C27) for any ω_p , which gives $R(\omega_p) + T(\omega_p) = 1$ for the normalized reflection and transmission spectra. The coherent cavity-matter coupling \hat{V}_a in Eq. (C29) does not alter this relation, but simply leads to a Rabi splitting in the strong coupling regime. In a more realistic scenario, where molecular dipoles decay radiatively into bound modes of the microcavity structure, conservation of photon flux can be stated as

$$|\langle \hat{\mathcal{E}}_{1}^{(+)} \rangle|^{2} + |\langle \hat{\mathcal{E}}_{2}^{(+)} \rangle|^{2} + |\langle \hat{\mathcal{E}}_{b}^{(+)} \rangle|^{2} = |\langle \hat{F}_{1} \rangle|^{2}, \tag{C37}$$

for any given ω_p . We have implicitly assumed that all boundmode fluorescence is collected in the far field. Normalizing the above equality by the input flux gives the usual definition the cavity absorption spectra

$$A = 1 - R - T. \tag{C38}$$

We thus show that the absorbed photon flux $A(\omega_p)$ at the driving frequency ω_p is determined by the normalized bound fluorescence intensity. In physical terms, fluorescence into bound modes of the microcavity attenuates the transmission and reflection of a driving laser. More generally, any process that leads to dipole decay, such as nonradiative molecular relaxation, would contribute to such field attenuation and contribute to the absorption spectra. However, we expect radiative relaxation to occur at a rate on the order of $\sqrt{N}\gamma_e$ due to the collective character of the electronic degrees of freedom in the strong cavity-matter coupling regime. Such size enhancements of the bound fluorescence rate may reduce the contribution of nonradiative processes to absorption.

APPENDIX D: SPECTRUM OF POLARITON FLUCTUATIONS

We derive here a general formula to compute two-time autocorrelations of the form

$$\langle \hat{O}_1(t+\tau)\hat{O}_2(t)\rangle$$
,

as needed in the computation of the leakage photoluminescence (LPL) of weakly driven cavities. The starting point of the derivation is the quantum regression formula [61,63]

$$\langle \hat{O}_1(t+\tau)\hat{O}_2(t)\rangle = \text{Tr}_S\{\hat{O}_1(0)e^{\mathcal{L}\tau}[\hat{O}_2(0)\hat{\rho}(t)]\},$$
 (D1)

where $\hat{\rho}(t)$ is the reduced density matrix of the system (organic cavity) that evolves according to $\hat{\rho}(t) = e^{\mathcal{L}t}\hat{\rho}(0)$, where $\hat{\rho}(0)$ is the initial state of the system and \mathcal{L} is the Liouville superoperator [61,63]. Using regression formula [Eq. (D1)] thus involves solving the master equation twice, first with respect to the absolute time t, starting from the initial condition $\hat{\rho}(0)$ in order to obtain the evolved state $\hat{\rho}(t)$, and then solving

$$\frac{d}{d\tau}\hat{\sigma}_t(\tau) = \mathcal{L}\,\hat{\sigma}_t(\tau),\tag{D2}$$

with respect to the delay time τ . This τ -dependent equation has the formal solution

$$\hat{\sigma}_t(\tau) = e^{\mathcal{L}\tau} \hat{\sigma}_t(0), \tag{D3}$$

for the *t*-dependent initial state $\hat{\sigma}_t(0) = \hat{O}_2\hat{\rho}(t)$. The required two-time correlation function in Eq. (D1) thus be rewritten as

$$\langle \hat{O}_1(t+\tau)\hat{O}_2(t)\rangle = \text{Tr}_S\{\hat{O}_1(0)\hat{\sigma}_t(\tau)\}. \tag{D4}$$

1. No-quantum-jump (NQJ) approximation

Assuming a standard Lindblad form for the Liovuille superoperator \mathcal{L} [63]

$$\mathcal{L}[\hat{\rho}] = -i[\hat{H}_S, \hat{\rho}] + \sum_{\alpha\beta} \gamma_{\alpha\beta} \left(\hat{L}_{\beta} \hat{\rho} \hat{L}_{\alpha}^{\dagger} - \frac{1}{2} \{ \hat{L}_{\alpha}^{\dagger} \hat{L}_{\beta}, \hat{\rho} \} \right), \tag{D5}$$

where $\gamma_{\alpha\beta}$ defines a decay matrix, \hat{L}_{α} are system jump operators associated with a model system-reservoir interaction, and \hat{H}_S is the system Hamiltonian (undriven or driven HTC model). The matrix $\gamma_{\alpha\beta}$ can be diagonalized together with a redefinition of the jump operators in order to obtain a master equation in Lindblad (diagonal) form, which preserves positivity of $\hat{\rho}$ [63]. For jump operators \hat{L}_{α} and $\hat{L}_{\alpha}^{\dagger}$ that are eigenoperators of the

system Hamiltonian \hat{H}_S we have $[\hat{H}_S, \hat{L}_{\alpha}^{\dagger} \hat{L}_{\beta}] = 0$, and we can write

$$\mathcal{L}[\hat{\rho}] = (\mathcal{L}_0 + \mathcal{L}_1)[\hat{\rho}], \tag{D6}$$

 \mathcal{L}_0 can be written as the non-Hermitian commutator

$$\mathcal{L}_0[\hat{\rho}] = -i(H_0\hat{\rho} - \hat{\rho}\hat{H}_0^{\dagger}),\tag{D7}$$

where

$$\hat{H}_0 = \hat{H}_S - \frac{i}{2} \sum_{\alpha\beta} \gamma_{\alpha\beta} \hat{A}_{\alpha}^{\dagger} \hat{A}_{\beta}, \tag{D8}$$

is an effective Hamiltonian with eigenstates $|\bar{\epsilon}_j\rangle$ that satisfy complex-eigenvalue equations $\hat{H}_0|\bar{\epsilon}_j\rangle = \bar{\epsilon}_j|\bar{\epsilon}_j\rangle$ and $\langle\bar{\epsilon}_j|\hat{H}_0^{\dagger} = \bar{\epsilon}_j^*\langle\bar{\epsilon}_j|$, with $\mathrm{Im}[\bar{\epsilon}_j] < 0$. This effective Hamiltonian is associated with the nonunitary evolution operator

$$\hat{U}_0(\tau) = \exp[-i\hat{H}_0\tau],\tag{D9}$$

such that the state norm decays with time as $\langle \bar{\epsilon}_j | \bar{\epsilon}_j \rangle_t = \exp[2\text{Im}[\bar{\epsilon}_j]t]$.

The recycling term in Eq. (D6) is given by

$$\mathcal{L}_{1}[\hat{\rho}] = \sum_{\alpha\beta} \gamma_{\alpha\beta} \, \hat{A}_{\beta} \hat{\rho} \hat{A}_{\alpha}^{\dagger}, \tag{D10}$$

and becomes the basis for our calculation of the emission and transmission spectra in organic cavities. When the system density matrix $\hat{\rho}(t)$ is such that the modified initial condition $\sigma_t(0)$ in Eq. (D3) satisfies, for every t, the equality

$$\mathcal{L}_1[\hat{\sigma}_t(0)] = 0, \tag{D11}$$

then the two-point correlation function in Eq. (D4) can be written as

$$\langle \hat{O}_1(t+\tau)\hat{O}_2(t)\rangle = \operatorname{Tr}_S\{\hat{O}_1 e^{\mathcal{L}_0 \tau} \hat{\sigma}_t(0)\}$$

= $\operatorname{Tr}_S\{\hat{O}_1 \hat{U}_0(\tau)\hat{\sigma}_t(0)\hat{U}_0^{\dagger}(\tau)\}.$ (D12)

Expanding the modified initial density matrix $\hat{\sigma}_t(0)$ in the eigenstates of \hat{H}_0 as

$$\hat{\sigma}_t(0) = \sum_{i:} \sigma_{ij}(t) |\bar{\epsilon}_i\rangle \langle \bar{\epsilon}_j|, \tag{D13}$$

allows us to write Eq. (D12) in the simple form

$$\langle \hat{O}_1(t+\tau)\hat{O}_2(t)\rangle = \sum_{ij} \langle \epsilon_i | \hat{O}_1 | \epsilon_j \rangle e^{-i\omega_{ij}\tau + \kappa_{ij}\tau} \sigma_{ij}(t), \quad (D14)$$

where $\omega_{ij} = \text{Re}[\bar{\epsilon}_i] - \text{Re}[\bar{\epsilon}_j]$ and $\kappa_{ij} = \text{Im}[\bar{\epsilon}_i] + \text{Im}[\bar{\epsilon}_j]$. The corresponding spectrum of fluctuations gives

$$S_{12}(\omega,t) = \operatorname{Re} \int_{0}^{\infty} d\tau \langle \hat{O}_{1}(t+\tau)\hat{O}_{2}(t)\rangle e^{i\omega\tau}$$

$$= \sum_{kij} \rho_{kj}(t) \langle \epsilon_{k}|\hat{O}_{2}^{\dagger}|\epsilon_{i}\rangle \langle \epsilon_{i}|\hat{O}_{1}|\epsilon_{j}\rangle \frac{\kappa_{ij}}{(\omega - \omega_{ij})^{2} + \kappa_{ij}^{2}},$$
(D15)

where in the last line we used

$$\sigma_{ij}(t) = \langle \epsilon_i | \hat{O}_2 \hat{\rho}(t) | \epsilon_j \rangle = \sum_i \langle \epsilon_i | \hat{O}_2 | \epsilon_k \rangle \rho_{kj}(t), \quad (D16)$$

with $\rho_{kj}(t) = \langle \epsilon_k | \hat{\rho}(t) | \epsilon_j \rangle$ being an element of the system density matrix in the eigenbasis of \hat{H}_0 . In the steady state

 $(t \to \infty)$, the fluctuations become stationary and the spectrum becomes independent of the absolute time t. It is reasonable to assume that in the steady state the system density matrix $\hat{\rho}$ becomes diagonal in the energy eigenbasis, i.e., $\hat{\rho} = \sum_j \rho_j |\epsilon_j\rangle\langle\epsilon_j|$. If in addition to the mixed character of the system state, the fluctuation operators satisfy $\hat{O}_1 = \hat{O}_2^{\dagger}$, which is the relevant case for cavity emission and absorption, the spectrum of fluctuations in Eq. (D15) simplifies even further to read

$$S(\omega) = \sum_{ij} \rho_j |\langle \epsilon_i | \hat{O}_2 | \epsilon_j \rangle|^2 \frac{\kappa_{ij}}{(\omega - \omega_{ij})^2 + \kappa_{ij}^2}, \quad (D17)$$

which is the form used in the main text to model the spectra of organic microcavities, under the approximation that $\text{Im}[\epsilon_i] \ll \text{Im}[\epsilon_j]$ when $|\epsilon_i\rangle$ is in the ground-state manifold and $|\epsilon_j\rangle$ is a polariton eigenstate of the Holstein-Tavis-Cummings model. For the Lindblad quantum master equation in Eq. (38), we thus have

$$\kappa_{ij} \approx \Gamma_j/2 = \frac{1}{2} \sum_i \gamma_{ij}.$$
(D18)

2. Validity of the NQJ approximation

For our purposes, we specialize the discussion to system states $\hat{\rho}(t)$ that involve *at most* one electronic excitation or photon in the cavity, but any possible number of purely vibrational excitations. We assume that at time t the system can be described by a state of the form

$$\hat{\rho}(t) = \hat{\rho}^{(0)}(t) + \hat{\rho}^{(1)}(t),$$
 (D19)

where

$$\hat{\rho}^{(0)}(t) = \sum_{ii'} \rho_{ii'}(t) |\epsilon_i\rangle \langle \epsilon_{i'}|$$
 (D20)

is the reduced density matrix of the system projected onto the ground-state manifold $|\epsilon_i\rangle$, and

$$\hat{\rho}^{(1)}(t) = \sum_{jj'} \rho_{jj'}(t) |\epsilon_j\rangle \langle \epsilon_{j'}|, \qquad (D21)$$

into the polariton manifold $|\epsilon_j\rangle$, following the notation convention in the main text for the HTC eigenstates. The ground manifold eigenstates states have the form

$$|\epsilon_i\rangle = |g_1g_2\dots g_N\rangle|0_c\rangle|\{v\}\rangle_i,$$
 (D22)

where $|0_c\rangle$ is the vacuum state of the cavity and $|\{v\}\rangle_i = |v_1v_2...v_N\rangle_i$ describes the vibrational eigenstate of each molecule in the ensemble in the electronic ground state $|g\rangle$. On the other hand, HTC polariton eigenstates can be written as

$$|\epsilon_j\rangle = b_j |\psi_j^e\rangle |0_c\rangle + c_j |\phi_j^g\rangle |1_c\rangle,$$
 (D23)

where $|\psi_j^e\rangle$ is an electron-vibration state with any number of vibrational excitations but at most one molecule in its excited electronic state $|e\rangle$, and $|\phi_j^g\rangle$ is a state with any number of vibrational excitations but with all molecules in the ground electronic state $|g\rangle$. For a cavity field near resonant with the bare molecular transition frequency, we have $|c_j|^2 \approx |b_j|^2 \approx 1/2$.

We now consider the action of the electronic lowering operator $\sigma_n^- \equiv |g_n\rangle\langle e_n|$, where *n* labels a molecule in the ensemble, and the cavity photon annihilation operator \hat{a} on

the one-quantum energy eigenstates in the form of Eq. (D23). For a dipole transition we have

$$\hat{\sigma}_n^- |\epsilon_j^{(1)}\rangle = b_j |\gamma_j^g\rangle |0_c\rangle = b_j \sum_k v_{jk} |\epsilon_k^{(0)}\rangle, \tag{D24}$$

where we defined $|\gamma_j^g\rangle \equiv \sigma_n^- |\psi_j^e\rangle$. For the cavity photon operator we have

$$\hat{a}\left|\epsilon_{j}^{(1)}\right\rangle = c_{j}\left|\phi_{j}^{g}\right\rangle\left|0_{c}\right\rangle = c_{j}\sum_{k}u_{jk}\left|\epsilon_{k}^{(0)}\right\rangle. \tag{D25}$$

Equations (D24) and (D25) show that the identities

$$\hat{a}^2 |\epsilon_i^{(1)}\rangle = (\hat{\sigma}_n^-)^2 |\epsilon_i^{(1)}\rangle = 0 \tag{D26}$$

hold for all one-quantum eigenstates $|\epsilon_j\rangle$ and molecule index n. Physically, since the operators $\hat{\sigma}_n$ and \hat{a} remove one quantum of electronic of cavity field energy, respectively, from the lightmatter system, leaving the state in the manifold spanned by the zero-quantum eigenstates $|\epsilon_i\rangle$, no further high-frequency de-excitations are allowed.

We illustrate the use of Eq. (D26) with an example. Consider the leakage photoluminescence (LPL) spectrum. In this case, we are interested in evaluating the two-point correlation function $\langle \hat{a}^{\dagger}(t+\tau)\hat{a}(t)\rangle$, for a dissipative cavity dynamics involving a recycling term of the form [61]

$$\mathcal{L}_1[\hat{\rho}] = \kappa \, \hat{a} \, \hat{\rho} \, \hat{a}^{\dagger}, \tag{D27}$$

where $\kappa > 0$ is the decay rate for an empty cavity. Condition (D11) for $\hat{O}_2 = \hat{a}$ thus reads

$$\mathcal{L}_1[\hat{a}\,\hat{\rho}] \equiv \kappa \,\hat{a}^2 \hat{\rho} \hat{a}^{\dagger} = \kappa \,\hat{a}^2 (\hat{\rho}^{(0)} + \hat{\rho}^{(1)}) \hat{a}^{\dagger} = 0.$$
 (D28)

where we have inserted our one-quantum ansatz for $\hat{\rho}$ from Eq. (D19) and used Eq. (D26). The validity of the condition in Eq. (D11) allows us to write the stationary LPL spectrum as

$$S_{LPL}(\omega) = \sum_{ij} \rho_j \left| \langle \epsilon_i | \hat{a} | \epsilon_j \rangle \right|^2 \frac{\kappa_{ij}}{(\omega - \omega_{ij})^2 + \kappa_{ij}^2}, \quad (D29)$$

which is a special case of Eq. (D17) for $\hat{O}_2 = \hat{a}$.

Contributions to the state $\hat{\rho}$ from two-quantum states $\hat{\rho}^{(2)}$ give $\mathcal{L}_1[\hat{a}\hat{\rho}] \neq 0$. In this case, the derived formula for $S_{LPL}(\omega)$ becomes inaccurate. Weak driving of the cavity, either coherent or incoherent, such that $\langle \hat{a}^{\dagger}\hat{a} \rangle \ll 1$ ensures that the one-quantum ansatz for $\hat{\rho}$ is appropriate to interpret the observable LPL spectrum.

APPENDIX E: ABSORPTION OF A WEAK DRIVING FIELD

We consider the driven Holstein-Tavis-Cummings (HTC) Hamiltonian $\hat{H}(t) = \hat{\mathcal{H}} + \hat{V}_p(t)$, where $\hat{\mathcal{H}}$ is the undriven HTC model in Eq. (1) and

$$\hat{V}_{p}(t) = \Omega_{p}(\hat{a}^{\dagger} e^{-i\omega_{p}t} + \hat{a} e^{i\omega_{p}t}) \tag{E1}$$

is the periodic driving term with frequency ω_p and a small amplitude $\Omega_p \ll \sqrt{N}\Omega \ll \omega_c$. The quantum master equation for the system density matrix now reads $\dot{\hat{\rho}} = \mathcal{L}[\hat{\rho}] + \mathcal{L}_p[\hat{\rho}]$, where $\mathcal{L}[\hat{\rho}]$ is the time-independent Liouville superoperator defined in Eq. (D6) and

$$\mathcal{L}_p[\hat{\rho}] = -i[\hat{V}_p(t), \hat{\rho}] \tag{E2}$$

is treated as a perturbation to the system dynamics. We expand the system state $\hat{\rho}$ as a perturbative expansion in the amplitude Ω_p of the form

$$\hat{\rho} \approx \hat{\rho}^{(0)} + \hat{\rho}^{(1)} + \hat{\rho}^{(2)},$$
 (E3)

where $\hat{\rho}^{(n)}$ is $O(\Omega_p^n)$ in the driving amplitude. Note the different notational meaning from Eq. (D19). We are interested in the population of the jth polariton eigenstate to second order in the driving amplitude, i.e., $\rho_j^{(2)} = \langle \epsilon_j | \hat{\rho}^{(2)}(t) | \epsilon_j \rangle$, subject to the initial condition

$$\hat{\rho}(0) = |G\rangle\langle G|,\tag{E4}$$

where $|G\rangle$ is the absolute ground state of the system. This choice is appropriate to describe an undriven cavity at room temperature $(k_b T \ll \omega_v)$.

The zeroth-order equations of motion in the HTC eigenbasis are given by Eq. (38), i.e.,

$$\frac{d}{dt}\hat{\rho}^{(0)} = \sum_{ij} \frac{\gamma_{ij}}{2} (2|\epsilon_i\rangle\langle\epsilon_j|\hat{\rho}^{(0)}|\epsilon_j\rangle\langle\epsilon_i| - \{|\epsilon_j\rangle\langle\epsilon_j|,\hat{\rho}^{(0)}\}). \tag{E5}$$

Since the initial condition in Eq. (E4) is a zero-energy eigenstate of the jump operator $|\epsilon_i\rangle\langle\epsilon_j|$, the zeroth order solution is $\rho_j^{(0)}=0=\rho_{ij}^{(0)}$ and $\rho_i=\delta_{Gi}$, where $\rho_{ij}=\langle\epsilon_i|\hat{\rho}|\epsilon_j\rangle$ is an optical coherence and $\rho_i=\langle\epsilon_i|\hat{\rho}|\epsilon_i\rangle$ is a vibrational population in the ground-state manifold.

We then proceed to the first-order equations of motion, which read

$$\dot{\rho}_i^{(1)} = \sum_{i:} \gamma_{ij} \rho_j^{(1)},\tag{E6}$$

$$\dot{\rho}_{j}^{(1)} = -\sum_{ij} \gamma_{i} \rho_{j}^{(1)},$$
 (E7)

$$\dot{\rho}_{ij}^{(1)} = -\kappa_{ij} \rho_{ij}^{(1)} + i \delta_{iG} V_{ij}(t),$$
 (E8)

where $\kappa_{ij} \approx \sum_{i'} \gamma_{i'j}/2$, ignoring the decay of states $|\epsilon_i\rangle$ in the ground-state manifold. The coherence equation carries a contribution from the perturbation in Eq. (E2), with $V_{ij}(t) = \langle \epsilon_i | \hat{V}_p(t) | \epsilon_j \rangle$. Given the initial condition in Eq. (E4), the equation for the first order coherence can be formally solved to give

$$\rho_{ij}^{(1)}(t) = i \,\delta_{iG} \int_0^t d\tau \, e^{-\kappa_{ij}(t-\tau)} \, V_{ij}(\tau). \tag{E9}$$

Proceeding to second order, we can write the polariton population equation as

$$\dot{\rho}_{j}^{(2)}(t) = -\sum_{i} \gamma_{ij} \rho_{j}^{(2)}(t) + i2 \operatorname{Im} \left\{ V_{jG}(t) \rho_{Gj}^{(1)}(t) \right\}, \quad \text{(E10)}$$

which can be formally solved using Eq. (E9) to read

$$\rho_j^{(2)}(t) = e^{-\Gamma_j} \rho_j^{(2)}(t) + \int_0^t dt' e^{-\Gamma_j(t-t')} K(t'), \qquad \text{(E11)}$$

where $\Gamma_j = \sum_{ij} \gamma_{ij}$ is the polariton decay rate and we defined the second-order kernel

$$K(s) = 2 \operatorname{Re} \left\{ \int_0^s d\tau \, e^{-\kappa_{Gj}(s-\tau)} \, V_{jG}(s) V_{Gj}(\tau) \right\}.$$
 (E12)

In the steady state $(t \to \infty)$, the first term in Eq. (E11) vanishes for all initial states $\hat{\rho}(0)$, so we ignore it. Inserting the definition in Eq. (E1) and integrating the kernel K(t') gives the polariton population

$$\rho_{j}^{(2)}(t) = 2|\Omega_{p}|^{2}|\langle G|\hat{a}|\epsilon_{j}\rangle|^{2}\operatorname{Re}\left\{\frac{1}{i\alpha_{j}}\left[\frac{1}{\Gamma_{j}} - \frac{e^{-\Gamma_{j}t}}{\Gamma_{j}}\right] - \left(\frac{e^{(\Gamma_{j} - i\alpha_{j})t}}{\Gamma_{i} - i\alpha_{j}} - \frac{1}{\Gamma_{i} - i\alpha_{j}}\right)\right\}e^{-\Gamma_{j}t}, \quad (E13)$$

where $\alpha_j \equiv (\omega_p - \omega_{Gj}) - i\kappa_{Gj}$. In the steady-state limit $t \to \infty$, only the first term in square brackets survives, giving the desired stationary polariton population

$$\rho_j^{(2)}(\infty) = \frac{2|\Omega_p|^2}{\Gamma_j} |\langle G|\hat{a}|\epsilon_j\rangle|^2 \frac{\kappa_{Gj}}{(\omega_p - \omega_{Gj})^2 + \kappa_{Gj}^2}.$$
 (E14)

The stationary polariton population ρ_j enters in the expression for the bound fluorescence spectra from Eq. (D17), with

 $\hat{O}_2 = \hat{\mu}^{(+)}$, which reads

$$S_{\hat{\mu}}(\omega) = \sum_{ij} \rho_j |\langle \epsilon_i | \hat{\mu}^{(+)} | \epsilon_j \rangle|^2 \frac{\kappa_{ij}}{(\omega - \omega_{ij})^2 + \kappa_{ij}^2}.$$
 (E15)

For ρ_j given by Eq. (E14), we integrate $S_{\hat{\mu}}$ over all emission frequencies ω to obtain the absorption spectra $A(\omega_p)$ from Eq. (44) to read

$$\frac{A(\omega_p)}{|\Omega_p|^2} = \sum_{ij} \left(\frac{\pi}{\Gamma_j}\right) \frac{|\langle G|\hat{a}|\epsilon_j\rangle|^2 \kappa_{Gj}}{(\omega_p - \omega_{Gj})^2 + \kappa_{Gj}^2} |\langle \epsilon_i|\hat{\mu}^{(+)}|\epsilon_j\rangle|^2,$$

where we have used a Lorentzian normalization relation. For decoherence due to radiative decay only, we have $\kappa_{Gj} \approx \Gamma_j/2$. However, it is possible to generalize the microscopic origin of the coherence decay rate κ_{Gj} by extending the master equation in Eq. (C32) in order to account for ultrafast electronic and vibrational relaxation processes that do not involve fluorescence.

- [1] D. G. Lidzey, D. D. C. Bradley, M. S. Skolnick, T. Virgili, S. Walker, and D. M. Whittaker, Strong exciton-photon coupling in an organic semiconductor microcavity, Nature (London) **395**, **53** (1998).
- [2] D. G. Lidzey, D. D. C. Bradley, T. Virgili, A. Armitage, M. S. Skolnick, and S. Walker, Room Temperature Polariton Emission from Strongly Coupled Organic Semiconductor Microcavities, Phys. Rev. Lett. 82, 3316 (1999).
- [3] D. G. Lidzey *et al.*, Photon-mediated hybridization of frenkel excitons in organic semiconductor microcavities, Science **288**, 1620 (2000).
- [4] P. A. Hobson, W. L. Barnes, D. G. Lidzey, G. A. Gehring, D. M. Whittaker, M. S. Skolnick, and S. Walker, Strong exciton-photon coupling in a low-*Q* all-metal mirror microcavity, Appl. Phys. Lett. **81**, 3519 (2002).
- [5] J. R. Tischler, M. S. Bradley, V. Bulovic, J. H. Song, and A. Nurmikko, Strong Coupling in a Microcavity Led, Phys. Rev. Lett. 95, 036401 (2005).
- [6] R. J. Holmes and S. R. Forrest, Strong exciton–photon coupling in organic materials, Org. Electron. 8, 77 (2007).
- [7] S. Kéna-Cohen, M. Davanço, and S. R. Forrest, Strong Exciton-Photon Coupling in an Organic Single Crystal Microcavity, Phys. Rev. Lett. 101, 116401 (2008).
- [8] S. Kena-Cohen and S. R. Forrest, Room-temperature polariton lasing in an organic single-crystal microcavity, Nat. Photon. 4, 371 (2010).
- [9] J. A. Hutchison *et al.*, Tuning the work-function via strong coupling, Adv. Mater. 25, 2481 (2013).
- [10] J. Bellessa *et al.*, Strong coupling between plasmons and organic semiconductors, Electronics **3**, 303 (2014).
- [11] T. Schwartz, J. A. Hutchison, C. Genet, and T. W. Ebbesen, Reversible Switching of Ultrastrong Light-Molecule Coupling, Phys. Rev. Lett. 106, 196405 (2011).
- [12] S. Kéna-Cohen, S. A. Maier, and D. D. C. Bradley, Ultrastrongly coupled exciton-polaritons in metal-clad organic semiconductor microcavities, Adv. Opt. Mater. 1, 827 (2013).
- [13] M. Mazzeo et al., Ultrastrong light-matter coupling in electrically doped microcavity organic light emitting diodes, Appl. Phys. Lett. 104, 233303 (2014).

- [14] A. Cacciola et al., Ultrastrong coupling of plasmons and excitons in a nanoshell, ACS Nano 8, 11483 (2014).
- [15] J. George et al., Ultra-strong coupling of molecular materials: Spectroscopy and dynamics, Faraday Discuss. 178, 281 (2015).
- [16] S. Gambino *et al.*, Ultrastrong light-matter coupling in electroluminescent organic microcavities, Appl. Mat. Today 1, 33 (2015).
- [17] J. P. Long and B. S. Simpkins, Coherent coupling between a molecular vibration and Fabry–Perot optical cavity to give hybridized states in the strong coupling limit, ACS Photon. 2, 130 (2015).
- [18] M. Muallem, A. Palatnik, G. D. Nessim, and Y. R. Tischler, Strong light-matter coupling between a molecular vibrational mode in a pmma film and a low-loss mid-ir microcavity, Ann. Phys. 528, 313 (2016).
- [19] J. George *et al.*, Liquid-phase vibrational strong coupling, J. Phys. Chem. Lett. 6, 1027 (2015).
- [20] A. Shalabney *et al.*, Coherent coupling of molecular resonators with a microcavity mode, Nat. Commun. **6** 5981 (2015).
- [21] P. Saurabh and S. Mukamel, Two-dimensional infrared spectroscopy of vibrational polaritons of molecules in an optical cavity, J. Chem. Phys. 144, 124115 (2016).
- [22] P. Andrew and W. L. Barnes, Förster energy transfer in an optical microcavity, Science **290**, 785 (2000).
- [23] J. Feist and F. J. Garcia-Vidal, Extraordinary Exciton Conductance Induced by Strong Coupling, Phys. Rev. Lett. 114, 196402 (2015).
- [24] J. Schachenmayer, C. Genes, E. Tignone, and G. Pupillo, Cavity-Enhanced Transport of Excitons, Phys. Rev. Lett. 114, 196403 (2015).
- [25] E. Orgiu *et al.*, Conductivity in organic semiconductors hybridized with the vacuum field, Nat. Mater. 14, 1123 (2015).
- [26] J. Yuen-Zhou, S. K. Saikin, T. Zhu, M. C. Onbasli, C. A. Ross, V. Bulovic, and M. A. Baldo, Plexciton Dirac points and topological modes, Nat. Commun. 7 11783 (2016).
- [27] F. Herrera *et al.*, Quantum nonlinear optics with polar Jaggregates in microcavities, J. Phys. Chem. Lett. **5**, 3708 (2014).

- [28] K. Bennett, M. Kowalewski, and S. Mukamel, Novel photochemistry of molecular polaritons in optical cavities, Faraday Discuss. **194**, 259 (2016).
- [29] M. Kowalewski, K. Bennett, and S. Mukamel, Non-adiabatic dynamics of molecules in optical cavities, J. Chem. Phys. 144, 054309 (2016).
- [30] M. Kowalewski, K. Bennett, and S. Mukamel, Cavity femtochemistry: manipulating nonadiabatic dynamics at avoided crossings, J. Phys. Chem. Lett. 7, 2050 (2016).
- [31] J. A. Hutchison *et al.*, Modifying chemical landscapes by coupling to vacuum fields, Angew. Chem. Int. Ed. 51, 1592 (2012).
- [32] B. S. Simpkins, K. P. Fears, W. J. Dressick, B. T. Spann, A. D. Dunkelberger, and J. C. Owrutsky, Spanning strong to weak normal mode coupling between vibrational and fabry–pérot cavity modes through tuning of vibrational absorption strength, ACS Photon. 2, 1460 (2015).
- [33] F. Herrera and F. C. Spano, Cavity-Controlled Chemistry in Molecular Ensembles, Phys. Rev. Lett. 116, 238301 (2016).
- [34] K. J. Vahala, Optical microcavities, Nature (London) 424, 839 (2003).
- [35] V. May and O. Kuhn, Charge and Energy Transfer Dynamics in Molecular Systems, 3rd ed., Vol. 35 (Wiley-VCH, Weinheim, Germany, 2011), p. 657.
- [36] V. M. Agranovich, M. Litinskaia, and D. G. Lidzey, Cavity polaritons in microcavities containing disordered organic semiconductors, Phys. Rev. B 67, 085311 (2003).
- [37] M. Litinskaya, P. Reineker, and V. M. Agranovich, Fast polariton relaxation in strongly coupled organic microcavities, J. Lumin. 110, 364 (2004).
- [38] M. Litinskaya, P. Reineker, and V. Agranovich, Excitonpolaritons in organic microcavities, J. Lumin. 119, 277 (2006).
- [39] D. M. Coles, P. Michetti, C. Clark, W. C. Tsoi, A. M. Adawi, J.-S. Kim, and D. G. Lidzey, Vibrationally assisted polaritonrelaxation processes in strongly coupled organic-semiconductor microcavities, Adv. Funct. Mater. 21, 3691 (2011).
- [40] T. Virgili, D. Coles, A. M. Adawi, C. Clark, P. Michetti, S. K. Rajendran, D. Brida, D. Polli, G. Cerullo, and D. G. Lidzey, Ultrafast polariton relaxation dynamics in an organic semiconductor microcavity, Phys. Rev. B 83, 245309 (2011).
- [41] T. Schwartz, J. A. Hutchison, J. Léonard, C. Genet, S. Haacke, and T. W. Ebbesen, Polariton dynamics under strong lightmolecule coupling, ChemPhysChem 14, 125 (2013).
- [42] J. A. Ćwik, P. Kirton, S. De Liberato, and J. Keeling, Excitonic spectral features in strongly coupled organic polaritons, Phys. Rev. A 93, 033840 (2016).
- [43] R. J. Holmes and S. R. Forrest, Strong Exciton-Photon Coupling and Exciton Hybridization in a Thermally Evaporated Polycrystalline Film of an Organic Small Molecule, Phys. Rev. Lett. 93, 186404 (2004).
- [44] L. Mazza, L. Fontanesi, and G. C. La Rocca, Organic-based microcavities with vibronic progressions: Photoluminescence, Phys. Rev. B **80**, 235314 (2009).
- [45] L. Fontanesi, L. Mazza, and G. C. La Rocca, Organic-based microcavities with vibronic progressions: Linear spectroscopy, Phys. Rev. B 80, 235313 (2009).

- [46] F. C. Spano, Optical microcavities enhance the exciton coherence length and eliminate vibronic coupling in j-aggregates, J. Chem. Phys. **142**, 184707 (2015).
- [47] M. A. Zeb, P. G. Kirton, and J. Keeling, Exact quantum states of the Holstein-Tavis-Cummings model, arXiv:1608.08929.
- [48] N. Wu, J. Feist, and F. J. Garcia-Vidal, When polarons meet polaritons: Exciton-vibration interactions in strongly-coupled organic microcavities, Phys. Rev. B **94**, 195409 (2016).
- [49] J. A. Ćwik, S. Reja, P. B. Littlewood, and J. Keeling, Polariton condensation with saturable molecules dressed by vibrational modes, Europhys. Lett. 105, 47009 (2014).
- [50] T. Holstein, Studies of polaron motion, part I. The molecularcrystal model, Ann. Phys. 8, 325 (1959).
- [51] F. C. Spano, The spectral signatures of frenkel polarons in hand j-aggregates, Acc. Chem. Res. 43, 429 (2010).
- [52] B. M. Garraway, The Dicke model in quantum optics: Dicke model revisited, Philos. Trans. R. Soc. London, Ser. A 369, 1137 (2011).
- [53] J. Galego, F. J. Garcia-Vidal, and J. Feist, Cavity-Induced Modifications of Molecular Structure in the Strong-Coupling Regime, Phys. Rev. X 5, 041022 (2015).
- [54] V. Agranovich and G. L. Rocca, Electronic excitations in organic microcavities with strong light–matter coupling, Solid State Commun. 135, 544 (2005).
- [55] F. Herrera and F. C. Spano, Dark vibronic polaritons and the spectroscopy of organic microcavities, Phys. Rev. Lett. 118, 223601 (2017).
- [56] R. Chikkaraddy, B. de Nijs, F. Benz, S. J. Barrow, O. A. Scherman, E. Rosta, A. Demetriadou, P. Fox, O. Hess, and J. J. Baumberg, Single-molecule strong coupling at room temperature in plasmonic nanocavities, Nature (London) 535, 127 (2016).
- [57] W. L. Barnes, Fluorescence near interfaces: The role of photonic mode density, J. Mod. Opt. 45, 661 (1998).
- [58] P. Michetti and G. C. La Rocca, Simulation of J-aggregate microcavity photoluminescence, Phys. Rev. B 77, 195301 (2008).
- [59] S. M. Barnett and P. Radmore, Methods in Theoretical Quantum Optics (Oxford University Press, Oxford, UK, 1997).
- [60] B. B. J. Matterson, J. M. Lupton, A. F. Safonov, M. G. Salt, W. L. Barnes, and I. D. W. Samuel, Increased efficiency and controlled light output from a microstructured light-emitting diode, Adv. Mater. 13, 123 (2001).
- [61] H. Carmichael, Statistical Mehods in Quantum Optics 1: Master Equations and Fokker-Planck Equations (Springer, Berlin, 1999).
- [62] F. C. Spano and S. Mukamel, Superradiance in molecular aggregates, J. Chem. Phys. 91, 683 (1989).
- [63] H. P. Breuer and F. Petruccione, *The Theory of Open Quantum Systems* (Oxford University Press, Oxford, UK, 2002).
- [64] A. Delga, J. Feist, J. Bravo-Abad, and F. J. Garcia-Vidal, Theory of strong coupling between quantum emitters and localized surface plasmons, J. Opt. **16**, 114018 (2014).
- [65] P. Törmä and W. L. Barnes, Strong coupling between surface plasmon polaritons and emitters: A review, Rep. Prog. Phys. 78, 013901 (2015).
- [66] B. Zhu, J. Schachenmayer, M. Xu, F. Herrera, J. G. Restrepo, M. J. Holland, and A. M. Rey, Synchronization of interacting quantum dipoles, New J. Phys. 17, 083063 (2015).

- [67] F. Beaudoin, J. M. Gambetta, and A. Blais, Dissipation and ultrastrong coupling in circuit qed, Phys. Rev. A 84, 043832 (2011).
- [68] Y. Wang, J. Zhang, C. Wu, J. Q. You, and G. Romero, Holonomic quantum computation in the ultrastrong-coupling regime of circuit QED, Phys. Rev. A 94, 012328 (2016).
- [69] W. L. Barnes and J. R. Sambles, Guided optical waves in Langmuir-Blodgett films of 22 tricosenoic acid, Surf. Sci. 177, 399 (1986).
- [70] D. Ballarini, M. De Giorgi, S. Gambino, G. Lerario, M. Mazzeo, A. Genco, G. Accorsi, C. Giansante, S. Colella, S. D'Agostino, P. Cazzato, D. Sanvitto, and G. Gigli, Polariton-induced enhanced emission from an organic dye under the strong coupling regime, Adv. Opt. Mater. 2, 1076 (2014).
- [71] F. C. Spano and H. Yamagata, Vibronic coupling in J-aggregates and beyond: A direct means of determining the exciton coherence length from the photoluminescence spectrum. J. Phys. Chem. B 115, 5133 (2011).

- [72] V. Savona, C. Piermarocchi, A. Quattropani, P. Schwendimann, and F. Tassone, Optical properties of microcavity polaritons, Phase Trans. 68, 169 (1999).
- [73] L. Knöll, S. Scheel, and D.-G. Welsch, Qed in dispersing and absorbing media, in *Coherence and Statistics of Photons and Atoms*, Wiley Series in Lasers and Applications, edited by J. Perina (Wiley-VCH, New York, 2001).
- [74] C. W. Gardiner and M. J. Collett, Input and output in damped quantum systems: Quantum stochastic differential equations and the master equation, Phys. Rev. A 31, 3761 (1985).
- [75] C. Ciuti and I. Carusotto, Input-output theory of cavities in the ultrastrong coupling regime: The case of time-independent cavity parameters, Phys. Rev. A 74, 033811 (2006).
- [76] H. A. Macleod, *Thin-Film Optical Filters*, 4th ed. (CRC Press, Boca Raton, FL, 2010).
- [77] D. Walls and G. J. Milburn, *Quantum Optics*, 2nd ed. (Springer-Verlag, Berlin, 2008), p. 425.